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978-0-521-83450-3 - Quantum Stochastic Processes and Noncommutative Geometry

Kalyan B. Sinha and Debashish Goswami

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