

Cambridge University Press

978-0-521-75307-4 - Soliton Equations and their Algebro-Geometric Solutions, Volume II:  
(1+1)-Dimensional Continuous Models

Fritz Gesztesy, Helge Holden, Johanna Michor and Gerald Teschl

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