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978-0-521-73902-3 - Input-Output Analysis: Foundations and Extensions, Second Edition

Ronald E. Miller and Peter D. Blair

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