

Cambridge University Press

978-0-521-73182-9 - Markov Chains and Stochastic Stability, Second Edition

Sean Meyn and Richard L. Tweedie

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Asterisks () mark sections from the first edition that have been revised or augmented in the second edition.*

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