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978-0-521-71514-0 - Non-equilibrium Statistical Mechanics and Turbulence: John Cardy,
Gregory Falkovich and Krzysztof Gawędzki

Edited by Sergey Nazarenko and Oleg V. Zaboronski

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