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Methods in Banach Space Theory

Proceedings of the V Conference
on Banach Spaces, Cáceres,
Spain, 13–18 September 2004

Edited by

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CAMBRIDGE
UNIVERSITY PRESS

Cambridge University Press & Assessment
978-0-521-68568-9 — Methods in Banach Space Theory
Edited by Jesus M. F. Castillo, William B. Johnson
Frontmatter
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CAMBRIDGE
UNIVERSITY PRESS

Shaftesbury Road, Cambridge CB2 8EA, United Kingdom
One Liberty Plaza, 20th Floor, New York, NY 10006, USA
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314–321, 3rd Floor, Plot 3, Splendor Forum, Jasola District Centre, New Delhi – 110025, India
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Cambridge University Press is part of Cambridge University Press & Assessment,
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www.cambridge.org
Information on this title: www.cambridge.org/9780521685689

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First published 2006

A catalogue record for this publication is available from the British Library

ISBN 978-0-521-68568-9 Paperback

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Picture: some like it fun. p. 358

Preface

In the end, mathematics is what matters. In addition to the contributors to this volume of proceedings, the Conference included talks by C. Benítez, F. Cobos, P. Domanski, G. Godefroy, W. B. Johnson, A. Molto, J. P. Moreno, P. L. Papini and R. Phelps among the main speakers, and Julio Flores, Yves Raynaud, F. Naranjo, José Orihuela, Pedro Martín, I. J. Cabrera, V. Montesinos, P. Hájek, Luis Oncina, G. Gruenhage, Fernando García, Vassilis Kanellopoulos, I. Villanueva, P. Bandyopadhyay, Sebastian Lajara, Diego Yañez, David Pérez-García, C. Michels, Bernardo Cascales, Pandelis Dodos, Antonio Pulgarín, M. Muñoz, José Rodríguez, Luz M. Fernández-Cabrera, Carmen Calvo, Juan Casado, Belmensnaoui Aqzzouz, Redouane Nourira, Antonio Martínez, Fernando Mayoral, Maria del Carmen Calderón Moreno, Luiza Amália de Moraes, J. A. Prado Bassas, My Hachem Lalaoui Rhali, Houcine Benabdellah, Rachid El Harti, Michael Stessin among the shorter talks.

The conference was organized, like this proceedings volume, in five sections,

- Geometrical methods
- Homological methods
- Topological methods
- Operator theory methods
- Function space methods

The idea was to organize Banach space theory (and related categories) according to the methods used to approach problems. Of course, the methods can overlap, and (fortunately) usually do, but typically one of the methods sticks out. This proceedings volume has been organized accordingly; so, in each of its five sections the reader will encounter survey and research papers describing the state-of-the-art in each of those areas. All together the sixteen papers depict a rather attractive panorama of modern infinite dimensional Banach space theory.

Acknowledgements

From September 13th to September 18th, 2004, the Banach space theory group of the Mathematics Department of the University of Extremadura played host to the V Conference on Banach spaces and related topics. The conference was sponsored by:

- Departamento de Matemáticas de la Uex
- Universidad de Extremadura
- Diputación de Cáceres
- Consejería de Educación de la Junta de Extremadura
- Caja de Extremadura

The editors of this proceedings volume express their gratitude to those organizations for financial support. The Junta de Extremadura must moreover be acknowledged for putting at our disposal the beautiful XVIth century palace “Complejo San Francisco”. We thank Cambridge University Press for making this volume proceedings a reality, and are grateful for the coordination efforts of Roger Astley and Catherine Appleton.

The conference united 86 participants from 14 countries, including leading specialists in the field. Thanks are due to the members of the Scientific Committee, Fernando Bombal, María Jesús Carro, Manuel González, Bob Phelps, and Angel Rodríguez Palacios, and to the main speakers of the conference for their generous participation. All related information can be found at the website <http://www.banachspaces.com/banach04>. Last but not least, on behalf of all the participants we thank the volunteer students for the truly outstanding effort they made throughout the conference, doing whatever had to be done with extra

smiles: Sandra Anes, Patricia Arjona, Javier Cabello, María Fejo, Ruth García,
José Navarro and Jesús Suárez.

