#### The Physics of Particle Detectors

This text provides a comprehensive introduction to the physical principles and design of particle detectors, covering all major detector types in use today. The book begins with a reprise of the size and energy scales involved in different physical processes. It then considers non-destructive methods, including the photoelectric effect, photomultipliers, scintillators, Cerenkov and transition radiation, scattering and ionization and the use of magnetic fields in drift and wire chambers. A complete chapter is devoted to silicon detectors. In the final part of the book, the author discusses destructive measurement techniques including Thomson and Compton scattering, Bremsstrahlung and calorimetry. Throughout the book, emphasis is placed on explaining the physical principles on which detection is based, and showing, by considering appropriate examples, how those principles are best utilized in real detectors. This approach also reveals the limitations that are intrinsic to different devices.

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# THE PHYSICS OF PARTICLE DETECTORS

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