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978-0-521-65992-5 - Rarefied Gas Dynamics: From Basic Concepts to Actual Calculations

Carlo Cercignani

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