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978-0-521-65817-1 - Elliptic Curves: Function Theory, Geometry, Arithmetic

Henry McKean and Victor Moll

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