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0521652340 - Introductory Statistics with Applications in General Insurance

I. B. Hossack, J. H. Pollard and B. Zehnwirth

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