

Index

Remember to look at the contents for larger topics. Abbreviations used in this index: m.g.f. = moment generating function; p.g.f. = probability generating function.

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