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0521632005 - Theory and Computation of Hydrodynamic Stability

W. O. Criminale, T. L. Jackson and R. D. Joslin

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