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0521604958 - Representations of Nilpotent Lie Groups and their Applications: Basic Theory and Examples, Part I

Lawrence J. Corwin and Frederick P. Greenleaf

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