Index of notations

The notations are listed in something like alphabetical order, which I do not propose to formalize in a detailed set of rules. Suffice it to say that greek letters are put near the associated roman letters on the whole, so far as the different 'alphabetical orders' allow, and that letters denoting variables are ignored so far as is possible.

The main reference given here is to the definition (in **bold** type), possibly with further references which I regard as particularly important. Where no definition is either given or referred to in the text, I have sometimes given such a reference in this index.

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