

Cambridge University Press

0521599237 - Representation Theory of Artin Algebras

Maurice Auslander, Idun Reiten and Sverre O. Smalø

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