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052158423X - Elements of the Representation Theory of Associative Algebras: Techniques  
of Representation Theory, Volume 1

Ibrahim Assem, Daniel Simson and Andrzej Skowronski

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