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0521574919 - Perturbation of the Boundary in Boundary-Value Problems of Partial  
Differential Equations

Dan Henry

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