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978-0-521-56511-0 - Topics in Advanced Econometrics: Estimation, Testing, and
Specification of Cross-Section and Time Series Models

Herman J. Bierens

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