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978-0-521-55890-7 - Theory of Distributions: A Non-technical Introduction

Ian Richards and Heekyung Youn

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