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978-0-521-55302-5 - Lévy Processes and Infinitely Divisible Distributions:
Corrected Printing with Supplement

Ken-Iti Sato

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