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978-0-521-53584-7 — Introduction to Banach Algebras, Operators, and Harmonic Analysis

H. Garth Dales , Pietro Aiena , Jörg Eschmeier , Kjeld Laursen , George A. Willis

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