

## Index

A page number printed in **bold** indicates that a definition or an important statement about the index entry appears on that page.

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