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If an entry is followed by a chapter number, then that notation is used only in that chapter. Otherwise, the notation may appear throughout the book.

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