Cambridge University Press			
978-0-521-46100-9 - Combinatorial	Games:	Tic-Tac-Toe	Theory
Jozsef Beck			
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