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Page numbers in **bold** type indicate the page on which the definition or definitive reference to the indexed term appears. The symbol “ G ” in the index refers to a minimal counterexample to the Odd Order Theorem.

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