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0521438284 - Weak Chaos and Quasi-Regular Patterns

G. M. Zaslavsky, R. Z. Sagdeev, D. A. Usikov and A. A. Chernikov

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