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This list contains, in addition to the papers quoted in the text, some relevant work not explicitly referred to, but no attempt at complete coverage has been made. In particular, the numerous papers on finite-dimensional division algebras, a branch much better documented, has for the most part been left aside.

Page references at the end of entries indicate the places in the text where the entry is quoted or implicitly referred to. Other references are listed after the author's name. Titles in Russian are marked (R).

A.1, 2, 3 refer to the author's *Algebra*, Second Edition, Volumes 1–3, J. Wiley and Sons, Chichester 1982, 1989, 1991.

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P. M. Cohn

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