

Plant Growth Curves The Functional Approach to

Plant Growth Analysis



'In general, curve fitting should be indulged in only when there are clear-cut objectives, and when the practitioner is aware of the pitfalls'.

(Williams, 1975)

"...omnes observationes nostrae propter instrumentorum sensuumque imperfectionem non sint nisi approximationes ad veritatem ..." ['all our observations, because of the imperfection of instruments and of the senses, are nothing more than approximations to the truth'].

(Gauss, 1809)



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The Functional Approach to Plant Growth Analysis

Roderick Hunt

B.Sc., Ph.D., M.I.Biol.

Independent Research Worker, Natural Environment Research Council Unit of Comparative Plant Ecology, Honorary Lecturer in Botany, University of Sheffield





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Preface

Plant growth curves in the special, but far from idiosyncratic, sense of this book are progressions of plant size against time. They have long occupied a vital place in plant science where studies on the performance of whole plants have often acted as the centre from which work at other levels of organization has radiated. The notion of change in size, too, with its fascination for the human mind and its indispensible involvement in biological sciences, has attracted statisticians from the earliest days of their subject and now occupies, through the agency of the fitted curve, a special place in the quantitative analysis of plant growth.

This book reviews the theory, practice and applications of fitted plant growth curves, a project I undertook both with excitement and with sadness; excitement, because this is the first time that a reasonably comprehensive coverage of this gratifyingly concise topic has been attempted, and sadness because, in view of the explosive development of the literature, it will in all probability also be the last, subsequent work necessarily involving some further subdivision. The time for viewing the subject as an entity is ripe, but this will soon pass as its twigs become branches, and so on.

Such matters as the book's background, anticipated readership and interrelationships with existing publications I cover in a separate introduction.

The work's existence owes much to many and my special thanks are due to Dr D. R. Causton for his friendly and critical co-operation at all stages of the project; to Dr G.C. Evans, who has on innumerable occasions given generously of his matchless experience; and to I.T. Parsons, a friend from school days and a valued collaborator over the last ten years.

My interest in plant growth analysis was first awakened at Sheffield by Professor A. R. Clapham. Since then, many friends and colleagues at the Universities of Bristol and Sheffield have shared with me their problems, ideas and successes in this and related fields: Dr J. F. Hope-Simpson, Dr E. I. Newman, C. R. Baines, the late Dr P. S. Lloyd, Dr J. Grace, the late Dr R. Law, Professor A. J. Willis, Dr I. H. Rorison, Dr J. P. Grime, Dr P. L. Gupta, Dr A. J. M. Baker, Dr H. Gretton, Dr S. B. Furness, Mrs. S. A. Fathy and Dr S. P. McGrath. Friends, collaborators and correspondents from many parts of the world have also brought me into contact with many diverse topics related to the study of plant growth, their numbers swollen by my good



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fortune in acting as Liaison Officer to the Natural Environment Research Council Unit of Comparative Plant Ecology at Sheffield. Chief among these are Professor F. A. Bazzaz, Dr M. J. Chadwick, Dr P. D. Crittenden, Dr J. G. P. Dirven, the late Dr A. P. Hughes, Dr R. G. Hurd, Dr B. C. Jarvis, H. T. Khong, Dr J. Květ Dr A. S. Mahmoud, Dr J. H. Mook, P. Sivan, Dr D. P. Stribley, Dr. A. Troughton and Dr F. I. Woodward. To these and all others not mentioned, my grateful thanks.

Over the years I have been helped by a series of willing and able assistants: R. J. Allen, Miss C. R. V. Rathey, Mrs H. J. Hucklesby and A. M. Neal while, almost throughout, Mrs A. M. N. Ruttle has provided incomparable secretarial support.

The permissions of the authors and publishers of the illustrative examples are gratefully acknowledged and I am indebted to the cited publication by S. Makridakis which prompted me to search the *Theoria motus* for the Gauss quotation which plays Charybdis to the Scylla of R. F. Williams opposite my title page. Dr D. R. Causton improved the whole text by his lengthy series of reader's comments and Dr G. C. Evans responded in characteristically farsighted style upon receipt of parts of Chapter 8. Errors and omissions remain my own and I will gladly receive due notice of these from readers, for which my thanks in advance.

Sheffield, 1982 R. H.



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