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978-0-521-40806-6 - Statistical Field Theory: Strong Coupling, Monte Carlo Methods,
Conformal Field Theory and Random Systems, Volume 2

Claude Itzykson and Jean-Michel Drouffe

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