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(B) refers to Bénard convection, (R-B) to Rayleigh–Bénard convection, and (T-V) to Taylor vortex. Bold numbers indicate where entries are defined.

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