

Cambridge University Press

0521400961 - Operator Algebras in Dynamical Systems: The Theory of Unbounded  
Derivations in C\*-Algebras

Shoichiro Sakai

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