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0521388112 - Helices and Vector Bundles: Seminaire Rudakov

A. N. Rudakov, A. I. Bondal, A. L. Gorodentsev, B. V. Karpov, M. M. Kapranov, S. A. Kuleshov,
A. V. Kvichansky, D. Yu. Nogin and S. K. Zube

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