

INDEX OF SYMBOLS

- | | | | |
|----------------------------|-----|-----------------------|-----|
| $ a, b, c, d $ | 8 | J | 8 |
| (η_-, η_+, s) | 130 | $L(a:k, \alpha)$ | 23 |
| (x, ξ) | 128 | $\Lambda_\alpha^s(E)$ | 2 |
| $b(0:a, \delta)$ | 4 | $\Lambda_\alpha(E)$ | 2 |
| D_a | 17 | μ_H | 162 |
| $d((x, \xi), (y, \eta))$ | 129 | μ_x | 52 |
| $dM(x, \xi)$ | 130 | $\mu_{x,s}$ | 49 |
| $d(E)$ | 3 | $\mu_{x,y,s}$ | 48 |
| dm_D | 176 | $N(r, x, y)$ | 18 |
| dm_x | 134 | $P(x, \xi)$ | 49 |
| dV | 17 | $\phi_\mu(x)$ | 97 |
| $d_x(\xi, \eta)$ | 55 | $Q(x)$ | 8 |
| $d\rho$ | 3 | R_α | 170 |
| $\Delta(x, a)$ (matrix) | 11 | $r(y:x, c)$ | 73 |
| $\Delta(a, \delta)$ (ball) | 4 | σ_x | 68 |
| Δ_2 | 89 | T_l | 26 |
| $\delta(\Gamma)$ | 21 | T_p | 27 |
| $g_s(x, y)$ | 45 | | |
| $g_s^*(y, y)$ | 48 | | |
| g_t | 134 | | |
| $\gamma^* \mu$ | 50 | | |
| h_t | 170 | | |
| $I(a:k, \alpha)$ | 5 | | |

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