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0521366372 - Banach Algebras and The General Theory of  $*$ -Algebras: Algebras and  
Banach Algebras, Volume I - Theodore W. Palmer

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