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978-0-521-32153-2 - Geometry and Interpolation of Curves and Surfaces

Robin J. Y. McLeod and M. Louisa Baart

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