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978-0-521-30042-1 - Singular-Perturbation Theory: An Introduction with Applications

Donald R. Smith

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