

Cambridge University Press

052129648X - Philosophy of Mathematics: Selected Readings, Second Edition

Edited by Paul Benacerraf and Hilary Putnam

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