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978-0-521-28882-8 - Mathematical Analysis: A Straightforward Approach, Second Edition

K. G. Binmore

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