

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

## LONDON MATHEMATICAL SOCIETY LECTURE NOTE SERIES

Managing Editor: Professor J.W.S. Cassels,  
Department of Pure Mathematics and Mathematical Statistics,  
16 Mill Lane, Cambridge CB2 1SB.

1. General cohomology theory and K-theory, P.HILTON
4. Algebraic topology, J.F.ADAMS
5. Commutative algebra, J.T.KNIGHT
8. Integration and harmonic analysis on compact groups, R.E.EDWARDS
9. Elliptic functions and elliptic curves, P.DU VAL
10. Numerical ranges II, F.F.BONSALL & J.DUNCAN
11. New developments in topology, G.SEGAL (ed.)
12. Symposium on complex analysis, Canterbury, 1973, J.CLUNIE  
& W.K.HAYMAN (eds.)
13. Combinatorics: Proceedings of the British Combinatorial Conference  
1973, T.P.McDONOUGH & V.C.MAVRON (eds.)
15. An introduction to topological groups, P.J.HIGGINS
16. Topics in finite groups, T.M.GAGEN
17. Differential germs and catastrophes, Th.BROCKER & L.LANDER
18. A geometric approach to homology theory, S.BUONCRISTIANO, C.P. ROURKE  
& B.J.SANDERSON
20. Sheaf theory, B.R.TENNISON
21. Automatic continuity of linear operators, A.M.SINCLAIR
23. Parallelisms of complete designs, P.J.CAMERON
24. The topology of Stiefel manifolds, I.M.JAMES
25. Lie groups and compact groups, J.F.PRICE
26. Transformation groups: Proceedings of the conference in the University  
of Newcastle-upon-Tyne, August 1976, C.KOSNIOWSKI
27. Skew field constructions, P.M.COHN
28. Brownian motion, Hardy spaces and bounded mean oscillations,  
K.E.PETERSEN
29. Pontryagin duality and the structure of locally compact Abelian  
groups, S.A.MORRIS
30. Interaction models, N.L.BIGGS
31. Continuous crossed products and type III von Neumann algebras,  
A.VAN DAELE
32. Uniform algebras and Jensen measures, T.W.GAMELIN
33. Permutation groups and combinatorial structures, N.L.BIGGS & A.T.WHITE
34. Representation theory of Lie groups, M.F. ATIYAH et al.
35. Trace ideals and their applications, B.SIMON
36. Homological group theory, C.T.C.WALL (ed.)
37. Partially ordered rings and semi-algebraic geometry, G.W.BRUMFIELD
38. Surveys in combinatorics, B.BOLLOBAS (ed.)
39. Affine sets and affine groups, D.G.NORTHCOTT
40. Introduction to Hp spaces, P.J.KOOSIS
41. Theory and applications of Hopf bifurcation, B.D.HASSARD,  
N.D.KAZARINOFF & Y-H.WAN
42. Topics in the theory of group presentations, D.L.JOHNSON
43. Graphs, codes and designs, P.J.CAMERON & J.H.VAN LINT
44.  $\mathbb{Z}/2$ -homotopy theory, M.C.CRABE
45. Recursion theory: its generalisations and applications, F.R.DRAKE  
& S.S.WAINER (eds.)
46. p-adic analysis: a short course on recent work, N.KOBLITZ
47. Coding the Universe, A.BELLER, R.JENSEN & P.WELCH
48. Low-dimensional topology, R.BROWN & T.L.THICKSTUN (eds.)
49. Finite geometries and designs, P.CAMERON, J.W.P.Hirschfield  
& D.R.Hughes (eds.)

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

50. Commutator calculus and groups of homotopy classes, H.J.BAUES
51. Synthetic differential geometry, A.KOCK
52. Combinatorics, H.N.V.TEMPERLEY (ed.)
53. Singularity theory, V.I.ARNOLD
54. Markov processes and related problems of analysis, E.B.DYNKIN
55. Ordered permutation groups, A.M.W.GLASS
56. Journées arithmétiques 1980, J.V.ARMITAGE (ed.)
57. Techniques of geometric topology, R.A.FENN
58. Singularities of smooth functions and maps, J.MARTINET
59. Applicable differential geometry, M.CRAMPIN & F.A.E.PIRANI
60. Integrable systems, S.P.NOVIKOV et al.
61. The core model, A.DODD
62. Economics for mathematicians, J.W.S.CASSELS
63. Continuous semigroups in Banach algebras, A.M.SINCLAIR
64. Basic concepts of enriched category theory, G.M.KELLY
65. Several complex variables and complex manifolds I, M.J.FIELD
66. Several complex variables and complex manifolds II, M.J.FIELD
67. Classification problems in ergodic theory, W.PARRY & S.TUNCEL
68. Complex algebraic surfaces, A.BEAUVILLE
69. Representation theory, I.M.GELFAND et al.
70. Stochastic differential equations on manifolds, K.D.ELWORTHY
71. Groups - St Andrews 1981, C.M.CAMPBELL & E.F.ROBERTSON (eds.)
72. Commutative algebra: Durham 1981, R.Y.SHARP (ed.)
73. Riemann surfaces: a view towards several complex variables, A.T.HUCKLEBERRY
74. Symmetric designs: an algebraic approach, E.S.LANDER
75. New geometric splittings of classical knots (algebraic knots), L.SIEBENMANN & F.BONAHON
76. Linear differential operators, H.O.CORDES
77. Isolated singular points on complete intersections, E.J.N.LOOIJENGA
78. A primer on Riemann surfaces, A.F.BEARDON
79. Probability, statistics and analysis, J.F.C.KINGMAN & G.E.H.REUTER (eds.)
80. Introduction to the representation theory of compact and locally compact groups, A.ROBERT
81. Skew fields, P.K.DRAXL
82. Surveys in combinatorics: Invited papers for the ninth British Combinatorial Conference 1983, E.K.LLOYD (ed.)
83. Homogeneous structures on Riemannian manifolds, F.TRICERRI & L.VANHECKE
84. Finite group algebras and their modules, P.LANDROCK
85. Solitons, P.G.DRAZIN
86. Topological topics, I.M.JAMES (ed.)
87. Surveys in set theory, A.R.D.MATHIAS (ed.)
88. FPF ring theory, C.FAITH & S.PAGE
89. An F-space sampler, N.J.KALTON, N.T.PECK & J.W.ROBERTS
90. Polytopes and symmetry, S.A.ROBERTSON
91. Classgroups of group rings, M.J.TAYLOR
92. Representation of rings over skew fields, A.H. SCHOFIELD
93. Aspects of topology, I.M.JAMES & E.H.KRONHEIMER (eds.)
94. Representations of general linear groups, G.D.JAMES
95. Low dimensional topology 1982: Proceedings of the Sussex Conference, 2-6 August 1982, R.A.FENN (ed.)
96. Diophantine equations over function fields, R.C.MASON
97. Varieties of constructive mathematics, D.S.BRIDGES & F.RICHMAN
98. Localization in Noetherian rings, A.V.JATEGAONKAR
99. Methods of differential geometry in algebraic topology, M.KAROUBI & C.LERUSTE
100. Stopping time techniques for analysts and probabilists, L.EGGHE

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

---

Aspects of topology

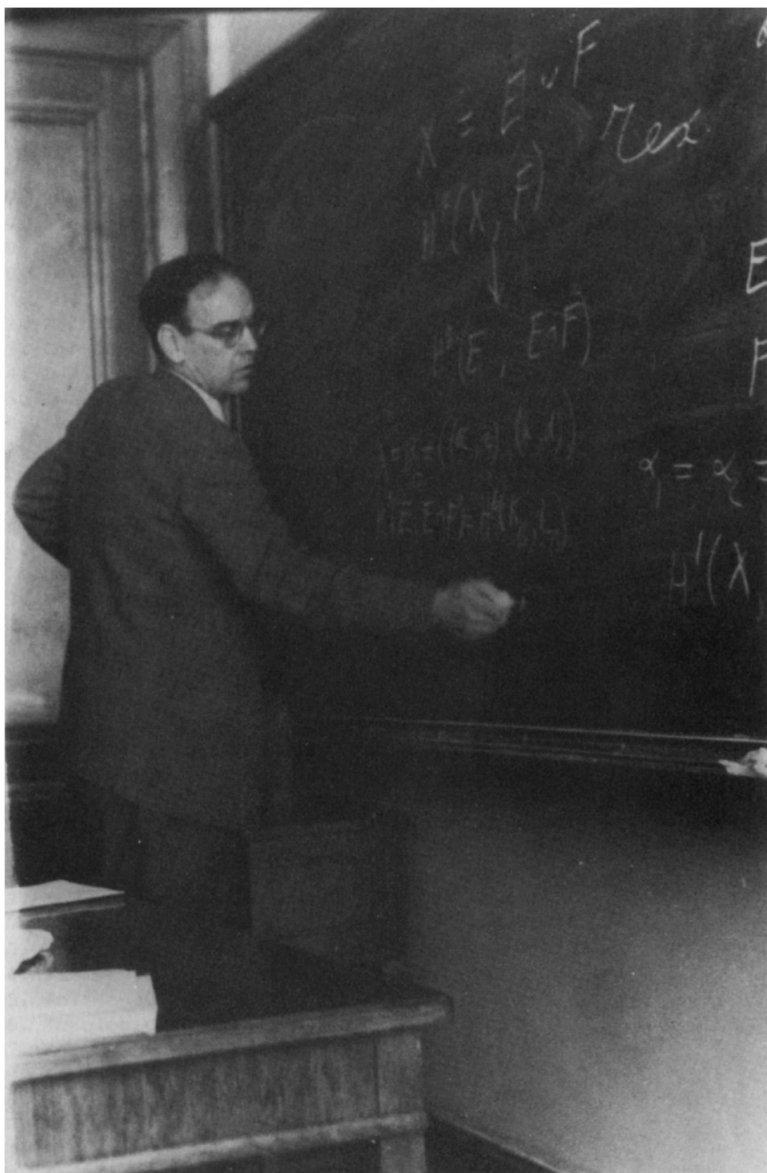
Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)



Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

London Mathematical Society Lecture Note Series: 93

# Aspects of topology

In memory of Hugh Dowker 1912 - 1982

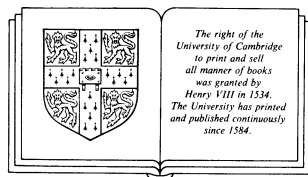
Edited by

I. M. JAMES

Savilian Professor of Geometry, Oxford University  
and

E. H. KRONHEIMER

Birkbeck College, University of London



CAMBRIDGE UNIVERSITY PRESS

Cambridge

London New York New Rochelle

Melbourne Sydney

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

---

CAMBRIDGE UNIVERSITY PRESS

Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paulo

Cambridge University Press

The Edinburgh Building, Cambridge CB2 8RU, UK

Published in the United States of America by Cambridge University Press, New York

[www.cambridge.org](http://www.cambridge.org)

Information on this title: [www.cambridge.org/9780521278157](http://www.cambridge.org/9780521278157)

© Cambridge University Press 1985

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written permission of Cambridge University Press.

First published 1985

Re-issued in this digitally printed version 2007

*A catalogue record for this publication is available from the British Library*

ISBN 978-0-521-27815-7 paperback

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

## CONTENTS

Obituary: Clifford Hugh Dowker Dona Strauss . . . . .	xi
Knot tabulations and related topics Morwen B. Thistlethwaite . . . . .	1
How general is a generalized space? Peter T. Johnstone . . . . .	77
A survey of metrization theory J. Nagata . . . . .	113
Some thoughts on lattice valued functions and relations M.W. Warner . . . . .	127
General topology over a base I.M. James . . . . .	141
$\kappa$ -Dowker spaces M.E. Rudin . . . . .	175
Graduation and dimension in locales J. Isbell . . . . .	195
A geometrical approach to degree theory and the Leray-Schauder index J. Dugundji . . . . .	211
On dimension theory B.A. Pasynkov . . . . .	227
An equivariant theory of retracts Sergey Antonian . . . . .	251
$P$ -embedding, $LC^n$ spaces and the homotopy extension property Kiiti Morita . . . . .	271
Special group automorphisms and special self-homotopy equivalences Peter Hilton . . . . .	281
Rational homotopy and torus actions Stephen Halperin . . . . .	293
Remarks on stars and independent sets P. Erdős and J. Pach . . . . .	307
Compact and compact Hausdorff A.H. Stone . . . . .	315
$T_1$ - and $T_2$ axioms for frames C.H. Dowker and D. Strauss . . . . .	325

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

---

#### CONTRIBUTORS

Professor S. Antonian, Department of Mathematics, State University of Yerevan, 375049 Yerevan-49, U.S.S.R.

Professor J. Dugundji, Department of Mathematics, University of Southern California, DRB 306, University Park, Los Angeles, California 90089-1113, U.S.A.

Professor P. Erdős, Mathematical Institute of Hungarian Academy of Sciences, Budapest, Reáltanoda u. 13-15, H-1053, Hungary.

Professor S. Halperin, Department of Mathematics, University of Toronto, Toronto, Canada M5S 1A1.

Professor P. Hilton, Division of Science and Mathematics, State University of New York at Binghamton, Binghamton, New York 13901, U.S.A.

Professor J. Isbell, Department of Mathematics, Wesleyan University, Middletown, Connecticut 06457, U.S.A.

Professor I.M. James, Mathematical Institute, University of Oxford, 24-29 St. Giles, Oxford OX1 3LB, England.

Dr P. Johnstone, Department of Pure Mathematics and Mathematical Statistics, University of Cambridge, 16 Mill Lane, Cambridge CB2 1SB, England.

Professor K. Morita, Department of Mathematics, Sophia University, Kioicho Chiyoda-ku, Tokyo 102, Japan.

Professor J. Nagata, Department of Mathematics, Osaka Kyoiku University, Tennoji, Osaka 543, Japan.

Professor J. Pach, Mathematical Institute of Hungarian Academy of Sciences, Budapest, Reáltanoda u. 13-15, H-1053, Hungary.

Professor B.A. Pasynkov, Moskovskii Univ., Mehmat, Moscow 117234, U.S.S.R.

Professor M.E. Rudin, Mathematics Department, University of Wisconsin-Madison, Van Vleck Hall, 480 Lincoln Drive, Madison, Wisconsin 53706, U.S.A.

Professor A.H. Stone, Department of Mathematics, Ray P. Hylan Building, University of Rochester, New York 14627, U.S.A.

Dr D. Strauss, Department of Pure Mathematics, University of Hull, 22-24 Newland Park, Hull HU5 2RD.

Dr M. Thistlethwaite, Polytechnic of the South Bank, London SE1 0AA, England.

Dr M. Warner, Department of Mathematics, City University, Northampton Square, London EC1V 0HB, England.



Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

---

#### NOTES

1. The photograph of Hugh Dowker was kindly provided by Yael Dowker.
2. The obituary notice, by Dona Strauss, is reprinted from the Bulletin of the London Mathematical Society, Volume 16, 1984.
3. The editors have made some minor alterations to the text of contributions by authors whose native language is other than english.
4. The final article was written by Dona Strauss on the basis of joint work by Hugh Dowker and herself.

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

## OBITUARY

## CLIFFORD HUGH DOWKER

Clifford Hugh Dowker was born in 1912 in Western Ontario, and grew up in a rural community, where his family owned a small farm. His ancestors on his father's side were of Yorkshire origin, while his mother was a McGregor of Scottish descent.

This rural background might appear unexpected for an important mathematician. Indeed, Hugh was the first Dowker to go to High School. Neither of his brothers had academic careers. His elder brother, Gordon, left school at thirteen and worked in the Canadian forests. His younger brother, Arthur, followed the family tradition of working as a farmer.

Hugh Dowker's first school was a one-room country school to which he had to walk a couple of miles. His next school was the High School in Parkhill, where the mathematics teacher appears to have had little understanding of the subject. Hugh was paid to stay in after school in order to teach mathematics to his teacher!

There was one teacher in Parkhill—not a mathematician—who seems to have had an important influence on Dowker. This was a teacher with a deep knowledge of wildlife, botany and geology, who took him and other pupils to the Muskoka Lakes and the Bruce Peninsula. This experience probably had a lasting effect on Dowker, who, throughout his life, displayed a keen interest in the countryside around him.

When Dowker was seventeen, he went to the University of Western Ontario, having been awarded a scholarship on the basis of his excellent examination results. He intended to be a school teacher. However, unexpectedly for himself and his family, his talents were to lead him into mathematics. This was a period of some penury for Dowker; the room that he shared with another student was heated by a chicken-coop heater, and he lived largely on tinned salmon and carrots—the cheapest foods available.

He studied a variety of subjects, including physics and economics, and received his BA degree in 1933. Then, because of his evident brilliance in mathematics, he was persuaded to continue his studies at the University of Toronto. After obtaining an MA there in the following year, he was advised to go to Princeton University to study under Lefschetz.

It was at Princeton that Dowker became fully aware of the power and beauty of mathematics, and that he became an active topologist, running one of Lefschetz' seminars. He obtained his Ph.D. there in 1938. Apart from Lefschetz, the mathematicians who were to have an important influence on Dowker included Alexandrov, Fox, Hurewicz and Steenrod.

He subsequently held a position as instructor at the University of Western Ontario, and was then an assistant to Von Neumann at the Princeton Institute for Advanced Study. He then went to Johns Hopkins University as an instructor. It was here that he met Yael Naim, whom he was to marry in 1944. Yael, at the time, was a young graduate student who had come to Johns Hopkins from Israel. She is herself a highly gifted mathematician, who was to become well-known for her work in ergodic

---

Received 22 February, 1984.

*Bull. London Math. Soc.*, 16 (1984), 535–541

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

theory. Dowker once remarked that all measure theorists marry topologists—this law being exemplified by the Dowkers, Rudins and Stones!

In 1943 Dowker was seconded to the United States Air Force as a civilian adviser, and carried out work on gunnery and the trajectories of projectiles, which took him to Libya and Egypt. Then, from 1943 to 1946, he and Yael both worked at the M.I.T. Radiation Laboratory. After the war he was an associate professor at Tufts, and then a visiting lecturer at Princeton and at Harvard.

This was the period of McCarthyism, when the atmosphere in North American Universities was very difficult. Several of Dowker's friends in the mathematical community were severely harassed, and one had been arrested. Hugh and Yael decided to leave North America. They came to England in 1950, where Yael had a post at the University of Manchester, and where Hugh was soon appointed to a readership in Applied Mathematics at Birkbeck College.

Although Dowker is famous for his work in the purest and most abstract branches of mathematics, it is a mark of his versatility that he deserved to hold a post as an applied mathematician. Indeed, he has made a real contribution to applied mathematics, through his work on projectiles and on servo-mechanisms [5].

In 1962 Dowker was appointed to a personal chair at Birkbeck College. He remained at Birkbeck until his retirement in 1979. He died in London in 1982, after a long and difficult illness against which he had struggled for seven years. He had been a member of the Society since 1951.

In manner, Dowker was reserved and gentle, with an innate dignity and a penetrating wit. He possessed a high degree of integrity and moral strength which enabled him to endure seven years of illness uncomplainingly. Although supremely tolerant towards others, he had only the highest standards of behaviour for himself. He was totally without ostentation or pretention and totally disinterested in wealth, honours or managerial power.

Hugh Dowker was unfailingly kind and generous and was always ready to spend time in aiding others. Over the course of some thirteen years, he and Yael did a great deal of work with children who were sent to them by the National Association for Gifted Children. The Dowkers were very committed to this work and were highly successful in it. They wrote an interesting joint paper [32], in which they describe how they had helped more than thirty gifted children—many of whom had difficulties in school—to experience the delight of mathematical discovery. It should not be thought that it was only with gifted children that Dowker was concerned. He had an affection for all young people and was known among his students for his helpfulness and patience. Even children in his neighbourhood would come to him for help with their homework.

Hugh and Yael were well known for their kindness and hospitality, which earned them many deep and lasting friendships in the mathematical community.

Dowker was widely travelled. In his early twenties he had twice “hoboed” across the United States and Canada, jumping on and off freight trains at suitable points. Later, as a mathematician, he held posts as a visiting professor in Russia, Israel, India and Canada. He also spent some time working on a kibbutz in Israel. He was able to speak Russian and knew some Georgian and some Hebrew. He loved the countryside, and often went walking or mountain-climbing in the national parks and in Switzerland.

That Dowker was impressively knowledgeable in mathematics was widely known; his letters and papers contain a wealth of answers to other mathematicians'

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

CLIFFORD HUGH DOWKER

xiii

questions. What might be less widely known, is that he had a deep knowledge of many subjects, including Georgian culture, the early history of Christian religions, the geography of many lands and localities and the history and anthropology of arithmetic in different societies. He always had a thorough knowledge of the history and culture of whatever area he happened to live in.

He had a deep love of mathematics, and continued to work even when he was weak and in pain. I visited him during the last days of his life, and was very moved by his determination to discuss mathematics even though he scarcely had the strength to speak.

He was a man who was respected and loved by his students, his many friends and the world-wide mathematical community.

#### *Mathematical work*

Dowker's mathematical work lay mainly in the field of topology. Although the number of his published papers is not large, they have been remarkably influential. His name is very widely quoted among topologists—indeed, it has been said that his best known paper [9] is one of the most frequently quoted in the whole of mathematics.

Dowker's papers are always striking, not only for their fundamental importance, but also for the elegance and clarity with which they are written. They contain a wealth of ingenious examples, often answering difficult problems posed by other mathematicians. He was constantly concerned to find the "right" basic definitions and axioms, and this led to his proving very general results under very few assumptions.

The results of his Ph.D. thesis were announced in [1] and presented, with additional material, in [3]. The theme of these papers was the extension of basic theorems in homotopy theory from compact metric to normal or paracompact spaces, a key role being played by the concept of uniform homotopy. [3] contains a pioneering exposition of Čech cohomology from a geometric point of view, and includes a proof of the surprising fact that the first Betti number of the real line is  $c$ . It also provides a proof of the important fact that the same covering dimension of a normal space is obtained whether finite, star-finite or locally finite covers are used. The techniques employed, involving the use of canonical maps to nerves of covers, led naturally to [6], in which it was shown that a canonical map of a space into the nerve of an arbitrary open covering exists if and only if the space is paracompact and normal. Although there are two different ways of topologising the nerve of a covering (called "geometric" and "natural"), they are shown to be equivalent in this context.

This observation led to a systematic study of metrisable topologies on infinite complexes in [10], in which the important fact is established that all the various reasonable topologies have the same homotopy type. In this paper, a question of J. H. C. Whitehead is answered by an example of two CW complexes whose product is not CW. The study of infinite complexes was continued in subsequent papers ([18, 21]). An interesting corollary of theorems proved in [21] is that isomorphic Euclidean complexes are homeomorphic.

Dowker's interest in locally finite covers led to [4], in which it was shown that paracompact metric spaces are precisely the spaces that can be embedded in Hilbert spaces. (It was not yet known that all metric spaces are paracompact.) This paper now provides a key step in the famous Bing–Nagata–Smirnov metrisation theorem.

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

[9] is probably Dowker's best known paper. This is the paper which introduced the important concept of countable paracompactness. In homotopy theory, the properties of a product space  $X \times I$ , where  $I$  denotes the closed unit interval, are fundamentally important. In [9], Hugh showed that  $X \times I$  is normal precisely in the case in which  $X$  is countably paracompact. He gave several striking and useful characterisations of countable paracompactness, and asked whether there were any normal spaces which failed to be countably paracompact. This question turned out to be one of the most challenging in general topology. It was finally answered twenty years later by Mary Ellen Rudin, who constructed an ingenious and intricate example of a normal space which was not countably paracompact. Spaces of this kind—which play a significant role in the study of non-metric spaces—are now known as “Dowker” spaces.

Dowker was constantly concerned with the fundamental definitions of homology and cohomology groups in general spaces. In [7] he showed how the Čech construction of direct and inverse limits can be used to deal with singular homology and cohomology. This work showed the identity of the Alexander and Čech cohomology groups in a wide class of spaces. In [8] he showed that the Eilenberg–Steenrod axioms were satisfied by Čech cohomology theory based on infinite open coverings. (It was known that the homotopy axiom failed to hold if finite covers were used.) The identity of the Čech and Vietoris homology groups and the Čech and Alexander cohomology groups was established in [11] for *arbitrary* spaces. A corollary of this is the fact that the Eilenberg–Steenrod axioms are satisfied by Alexander cohomology theory.

In [20, 22, 23], Dowker developed results in excision theory. In [20] he gave very general conditions for the strong excision property to hold for Čech cohomology. He also showed that some conditions, going beyond normality, are needed, thus proving a conjecture due to A. D. Wallace.

An interest in the extension of maps was implicit in [2, 3] and developed further in [12, 17, 18]. Dowker's main contribution was given in [17], where he gave very general conditions sufficient for extensibility, and gave criteria for spaces to be ANR and NES (neighbourhood extension) spaces. In an earlier paper [12], he had improved and generalised Hanner's characterisation of the separable metric spaces which are ANRs for normal spaces, and had extended it to non-separable spaces.

Dimension theory was a recurring theme in Dowker's work. [14] contains a thorough study of large inductive dimension (Ind) in completely normal spaces, and introduces the slightly more restrictive class of totally normal spaces, to which many of the principal theorems of classical dimension theory are extended. This study was continued in [15], where the subset theorem is extended to totally normal spaces. In this paper, Dowker shows that local dimension and dimension coincide in a wide class of spaces, and gives an example of a normal space in which they differ. In [19] it is shown that the dimension of a metric space can be defined in terms of a sequence of open covers satisfying the condition that the closures of the sets in the  $(i+1)$ -st cover form a refinement of the  $i$ -th cover. This paper also contains a new proof of the Katětov–Morita theorem which states that dim and Ind coincide for metric spaces.

[24] contains a generalisation of the concepts of proximity and uniformity, in which symmetry is not required. By discarding the property of symmetry, it becomes possible to define quotient, open and closed maps. Product structures are also defined and investigated. A question of Smirnov is answered by an example of a (symmetric) proximity space which has no finest consistent (symmetric) uniformity.

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

In joint papers with myself, published from 1966 onwards, Dowker did pioneering work in the study of frames. A frame is a complete lattice which satisfies the infinite distributivity condition:  $x \wedge \bigvee_a x_a = \bigvee_a (x \wedge x_a)$ . Lattices of this kind are significant in topology, as the lattice formed by the open subsets of a topological space is an example of a frame. They are also significant in other fields; for example, they furnish models for intuitionist logic. In recent years, they have aroused interest because of their applications in sheaf theory and in the new field of topos theory. Dowker was responsible for establishing some of the basic features of the category of frames, including the properties of quotients and co-products. (It should be noted that some of these ideas were developed independently by other mathematicians, including J. R. Isbell.)

[34] gives an indication of the versatility of Dowker's work. In this paper, written with M. Thistlethwaite, a complete classification of all 12,765 knots with at most thirteen crossings is given. The authors pioneered the use of the computer for the purpose of tabulating knots, and developed some strikingly ingenious new techniques.

Dowker was also interested in the general theory of categories. In [26] he showed how the connecting morphism of homology theory arises from a functor definable in any abelian category. In his final paper [35], written during the last weeks of his life, he proved the interesting fact that two categories must be isomorphic if there are functors between them which are injective on objects and have composites naturally equivalent to the identity functors.

Finally Dowker's influential lectures on sheaf theory [16] should be mentioned among his publications. They provide a very clear and careful exposition of the subject, with a wealth of illustrative examples, and were for some years the only source for several important results about sheaves and sheaf cohomology. Mathematicians, who are now experts in sheaf theory, have told me that it was these lecture notes which first awakened their interest in the subject.

This description of Dowker's mathematical work is not exhaustive. His command of mathematics was so wide that he has contributed to fields of which I am unaware. For example, I have recently learned of a theorem in pure geometry which bears his name.

#### *Acknowledgements*

I wish to express my gratitude to the many friends who have written to me about Hugh Dowker's life and work. I am particularly grateful to Yael Dowker, who has spent many hours in talking to me about him, and to Gordon Dowker, who sent me a very long and very interesting letter about his brother's childhood. I am also most grateful to Arthur Stone, who sent me an invaluable assessment of Dowker's mathematical work. A great deal of the account that I have given above, is, in fact, due to him, as I often felt unable to improve on his formulation.

#### *Bibliography*

1. 'Hopf's Theorem for non-compact spaces', *Proc. Nat. Acad. Sci. U.S.A.*, 23 (1937), 293-294.
2. 'On minimum circumscribed polygons', *Bull. Amer. Math. Soc.*, 50 (1944), 120-122 [*Math. Rev.* 5, #153 (John)].



Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

CLIFFORD HUGH DOWKER

xvi

3. 'Mapping theorems for non-compact spaces', *Amer. J. Math.*, 69 (1947), 200–242 [*Math. Rev.* 8, #594 (Freudenthal)].
4. 'An imbedding theorem for paracompact metric spaces', *Duke Math. J.*, 14 (1947), 639–645 [*Math. Rev.* 9, #196 (Dieudonné)].
5. (with R. Phillips) Chapter VIII, *Theory of servo-mechanisms* (McGraw Hill, 1947), 340–360. (Publication of the M.I.T. Radiation Laboratory.)
6. 'An extension of Alexandroff's mapping theorem', *Bull. Amer. Math. Soc.*, 54 (1948), 386–391 [*Math. Rev.* 9, #523 (Dieudonné)].
7. (with W. Hurewicz and J. Dugundji) 'Connectivity groups in terms of limit groups', *Ann. of Math.*, 49 (1948), 391–406 [*Math. Rev.* 9, #606 (Freudenthal)].
8. Čech cohomology theory and the axioms', *Ann. of Math.* (2), 51 (1950), 278–292 [*Math. Rev.* 11, #450 (Freudenthal)].
9. 'On countably paracompact spaces', *Canad. J. Math.*, 3 (1951), 219–224 [*Math. Rev.* 13, #264 (A. H. Stone)].
10. 'Topology of metric complexes', *Amer. J. Math.*, 74 (1952), 555–577 [*Math. Rev.* 13, #965 (Spanier)].
11. 'Homology groups of relations', *Ann. of Math.* (2), 56 (1952), 84–95 [*Math. Rev.* 13, #967 (Spanier)].
12. 'On a theorem of Hanner', *Ark. Mat.*, 2 (1952), 307–313 [*Math. Rev.* 14, #296 (Michael)].
13. 'A problem in set theory', *J. London Math. Soc.*, 27 (1952), 371–374 [*Math. Rev.* 13, #924 (Gustin)].
14. 'Inductive dimension of completely normal spaces', *Quart. J. Math., Oxford Ser.* (2), 4 (1953), 267–281 [*Math. Rev.* 16, #157 (Katětov)].
15. 'Local dimension of normal spaces', *Quart. J. Math. Oxford Ser.* (2), 6 (1955), 101–120 [*Math. Rev.* 19, #157 (M. Henriksen)].
16. *Lectures on sheaf theory*. Notes by S. V. Adavi and N. Ramabhadran (Tata Institute of Fundamental Research, Bombay, 1956, v+212+iv+iii pp. mimeographed) [*Math. Rev.* 19, #301 (M. F. Atiyah)].
17. 'Homotopy extension theorems', *Proc. London Math. Soc.* (3), (1956), 100–116 [*Math. Rev.* 17, #518 (J. Dugundji)].
18. 'Imbedding of metric complexes', *Algebraic geometry and topology*, A symposium in honour of S. Lefschetz (Princeton University Press, Princeton, N.J., 1957), pp. 239–242 [*Math. Rev.* 18, #920 (J. Dugundji)].
19. (with W. Hurewicz) 'Dimension of metric spaces', *Fund. Math.*, 43 (1956), 83–88 [*Math. Rev.* 18, #56 (Haskell Cohen)].
20. 'The excision theorem' (Russian), *Dokl. Akad. Nauk SSSR*, 125 (1959), 1190–1192 [*Math. Rev.* 21, #3840 (Isbell)].
21. 'Affine and Euclidean complexes' (Russian), *Dokl. Akad. Nauk SSSR*, 128 (1959), 655–656 [*Math. Rev.* 22, #8483 (Kahn)].
22. 'The Kolmogorov–Aleksandrov duality theorem' (Russian), *Mat. Sb. (N.S.)*, 50 (92) (1960), 247–255 [*Math. Rev.* 22, #12518 (Kahn)].
23. 'The map excision theorem' (Russian), *Soobshch. Akad. Nauk. Gruz. SSR*, 24 (1960), 649–654 [*Math. Rev.* 24, #A1124 (Isbell)].
24. 'Mapping of proximity structures', *General topology and its relations to modern analysis and algebra*, Proc. Sympos., Prague, 1961 (Academic Press, New York), pp. 139–141; Publ. House Czech. Acad. Sci., Prague; 1962 [*Math. Rev.* 26, #4312 (Krishnan)].
25. (with Dona Papert Strauss) 'Quotient frames and subspaces', *Proc. London Math. Soc.* (3), 16 (1966), 275–296 [*Math. Rev.* 34, #2510 (D. F. Brown)].
26. 'Composite morphisms in abelian categories', *Quart. J. Math. Oxford Ser.* (2), 37 (1966), 98–105 [*Math. Rev.* 34, #2652 (A. Heller)].
27. (with D. P. Strauss) 'On Urysohn's Lemma', *General topology and its relations to modern analysis and algebra, II*, Proc. Second Prague Topological Sympos., 1966 (Academia, Prague, 1967), pp. 111–114 [*Math. Rev.* 39, #108 (O. Frink)].
28. (with D. P. Strauss) 'Separation axioms for frames', *Topics in topology*, Proc. Colloq., Keszthely, 1972, *Colloq. Math. Soc. Janos Bolyai*, 8 (North Holland, Amsterdam, 1974), pp. 223–240 [*Math. Rev.* 52, #15360, 54D10 (06A23) (E. P. Rozycki)].
29. (with D. P. Strauss) 'Paracompact frames and closed maps', *Symposia Mathematica, Vol. XVI*, Convegno Sulla Topologia Isiemistica e Generale, Indam, Rome, 1973 (Academic Press, London, 1975), pp. 93–116 [*Math. Rev.* 53, #14411 54D20 (54F05, 06A23) (Stephen Willard)].
30. (with D. Strauss) 'Products and sums in the category of frames', *Categorical topology*, Proc. Conf. Mannheim, 1975, Lecture Notes in Mathematics 540 (Springer, Berlin, 1976), pp. 208–219 [*Math. Rev.* 55, #11216, 54F05 (E. J. Braude)].
31. (with D. Strauss) 'Sums in the category of frames', *Houston J. Math.*, 3 (1977), no. 1, 17–32. [*Math. Rev.* 56, #1275, 54F05 (06A23) (Stephen Willard). See also Problems in Topology *Math. Rev.* 50, #8399].
32. (with Yael Dowker) 'Helping gifted children with mathematics', *Journal of the gifted child*, No. 1, I (1979), 52–66.
33. (with M. Thistlethwaite) 'On the classification of knots', *Comptes Rendus Mathématiques de l'Académie de Science (Royal Soc. of Canada)*, vol. VI 2, (1982), 129–131.

Cambridge University Press

978-0-521-27815-7 - Aspects of Topology: In Memory of Hugh Dowker 1912-1982

Edited by I. M. James and E. H. Kronheimer

Frontmatter

[More information](#)

CLIFFORD HUGH DOWKER

xvii

34. (with M. Thistlethwaite) 'Classification of knot projections', *Topology and its applications*, 16 (1983), 19–31.
35. 'Isomorphism of categories', *J. Pure Appl. Algebra*, 27 (1983), 205–206.
36. (with D. Strauss) ' $T_1$ - and  $T_2$ -axioms for frames', *Aspects of topology* (Cambridge University Press), to appear.

Department of Pure Mathematics,  
The University of Hull,  
22–24 Newland Park,  
Hull HU5 2DW,  
England.

D. STRAUSS