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978-0-521-21512-1 - Brownian Motion, Hardy Spaces and Bounded Mean Oscillation

K. E. Petersen

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For F. A. P. and E. A. P.

Limits we did not set condition all we do.

Matthew Arnold

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