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978-0-521-18801-2 - Association Schemes Designed Experiments, Algebra and Combinatorics

R. A. Bailey

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