

Distillation Theory and Its Application to Optimal Design of Separation Units

Distillation Theory and Its Application to Optimal Design of Separation Units presents a clear, multidimensional, geometric representation of distillation theory that is valid for all types of distillation columns for all splits, column types, and mixtures. This representation answers such fundamental questions as:

- What are the feasible separation products for a given mixture?
- What minimum power is required to separate a given mixture?
- What minimum number of trays is necessary to separate a given mixture at a fixed-power input?

Methods of the general geometric theory of distillation, encoded in software, provide quick and reliable solutions to problems of flowsheet synthesis and to optimal design calculations. DistillDesigner software allows refinement and confirmation of the algorithms of optimal design.

This book is intended for students and specialists in the design and operation of separation units in the chemical, pharmaceutical, food, wood, petrochemical, oil-refining, and natural gas industries, and for software designers.

Felix B. Petlyuk, Ph.D., D.Sc., has worked in the petrochemical engineering and oil-refining industries for more than 40 years. He currently works for the engineering firm ECT Service in Moscow.



CAMBRIDGE SERIES IN CHEMICAL ENGINEERING

Series Editor:

Arvind Varma, Purdue University

Editorial Board:

Alexis T. Bell, *University of California, Berkeley*John Bridgwater, *University of Cambridge*Edward Cussler, *University of Minnesota*L. Gary Leal, *University of California, Santa Barbara*Massimo Morbidelli, *ETH*, *Zurich*Stanley I. Sandler, *University of Delaware*Michael L. Shuler, *Cornell University*

Books in the Series:

E. L. Cussler, Diffusion: Mass Transfer in Fluid Systems, Second Edition

Liang-Shih Fan and Chao Zhu, Principles of Gas-Solid Flows

Hasan Orbey and Stanley I. Sandler, Modeling Vapor-Liquid Equilibria: Cubic Equations of State and Their Mixing Rules

T. Michael Duncan and Jeffrey A. Reimer, *Chemical Engineering Design and Analysis: An Introduction*

John C. Slattery, Advanced Transport Phenomena

A. Varma, M. Morbidelli, and H. Wu, Parametric Sensitivity in Chemical Systems

M. Morbidelli, A. Gavriilidis, and A. Varma, Catalyst Design: Optimal Distribution of Catalyst in Pellets, Reactors, and Membranes

E. L. Cussler and G. D. Moggridge, Chemical Product Design

Pao C. Chau, Process Control: A First Course with MATLAB®

Richard Noble and Patricia Terry, *Principles of Chemical Separations with Environmental Applications*

Rodney Fox, Computational Models for Turbulent Reacting Flows



Distillation Theory and Its Application to Optimal Design of Separation Units

F. B. Petlyuk





> CAMBRIDGE UNIVERSITY PRESS Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paulo, Delhi, Tokyo, Mexico City

Cambridge University Press
The Edinburgh Building, Cambridge CB2 8RU, UK

Published in the United States of America by Cambridge University Press, New York

www.cambridge.org Information on this title: www.cambridge.org/9780521174060

© F. B. Petlyuk 2004

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written permission of Cambridge University Press.

First published 2004 First paperback edition 2011

A catalogue record for this publication is available from the British Library

Library of Congress Cataloguing in Publication data

Petlyuk, F. B. (Felix B.), 1934-

Distillation theory and its application to optimal design of separation units / F. B. Petlyuk.

p. cm. – (Cambridge series in chemical engineering) Includes bibliographical references and index.

ISBN 0-521-82092-8 (hardback)

1. Distillation. 2. Distillation apparatus - Design and construction.

1. Title. 11. Series.

TP156.D5P45 2004 660′.28425 – dc22

2003058496

ISBN 978-0-521-82092-9 Hardback ISBN 978-0-521-17406-0 Paperback

Cambridge University Press has no responsibility for the persistence or accuracy of URLs for external or third-party internet websites referred to in this publication, and does not guarantee that any content on such websites is, or will remain, accurate or appropriate.



Contents

	Prefa	ce	page xiii
	Ackn	owledgments	xvii
	Nome	enclature	xix
١.	Phase	e Equilibrium and Its Geometric Presentation	1
	1.1	Introduction	1
	1.2	Concentration Space	1 3 5
	1.3	Phase Equilibrium of Binary Mixtures	3
	1.4	Phase Diagrams of Three-Component Mixtures	
	1.5		8
	1.6	Matrix Description of the Multicomponent Mixture Residue	
		Curve Structure	10
	1.7	, , , , , , , , , , , , , , , , , , , ,	12
	1.8		15
		Conclusion	17
		Questions	18
	1.11	Exercises with Software References	18 18
<u>.</u>		Concepts of Distillation	20
	2.1	1	20
		.1. Description of Distillation Process	21
		.2. System of Algebraic Equations of Distillation	22
	2.2	Geometric Interpretation of Binary Distillation: Reflux and the	22
	2.2	Number of Trays 1. McCaba Thiala Diagram	23 23
		 McCabe-Thiele Diagram Influences of Nonideality 	24
	2.3	Geometric Interpretation of Multicomponent Mixture	24
	2.3	Distillation: Splits	25
	2.4	*	26
	2.5		27
	2.6	3	29
		.1. Binary Distillation	29
		2. Distillation of Three-Component Mixtures	31
			vii



VIII	Contents

	2.7	Adiabatic, Nonadiabatic, and Reversible Distillation	32
	2.8	Separation of Azeotropic Mixtures by Distillation Under Two	
		Pressures or Heteroazeotropic and Extractive Distillation	35
	2.9	Is Process Opposite to Distillation Process Possible?	36
	2.10	Mixtures with Limited and Unlimited Separability	37
		The Problem of Designing Distillation Units	38
	2.12	Questions	38
		References	39
3.	-	tories of Distillation in Infinite Columns Under Infinite Reflux	40
		Introduction	40
	3.2	Analogy Between Residue Curves and Distillation Trajectories Under Infinite Reflux	41
	3.3	Distillation Trajectories of Finite and Infinite Columns at Set	41
	3.3	Feed Composition	43
	3.3.1	. Dimensionality of Product Composition Regions for Finite	15
		and Infinite Columns	43
	3.3.2	2. Product Composition Regions for Ideal Three-Component	
		Mixtures	44
	3.3.3	3. Product Composition Regions for Ideal Four-Component	
	2.2	Mixtures	45
		Feasible Splits for Ideal Mixtures	47
	3.3.3	5. Product Composition Regions for Azeotropic Three-Component Mixtures	48
	3.4	Rule for the Checkup of Azeotropic Mixtures Separability at	40
	<i>.</i>	$R = \infty$ and $N = \infty$	52
	3.4.1	. Distillation Trajectories Location at $R = \infty$ and $N = \infty$	52
		2. Application of the Rule of Connectedness	53
		3. <i>n</i> -Component Mixture	55
		Feasible Splits at $R = \infty$ and $N = \infty$	57
	3.5.1	. Method of Product Simplex for Distillation Subregions	70
	250	(m = n) 2. Method of Product Simplex for Distillation Subregions	59
	3.3.2	(m > n)	61
	3.5.3		63
	3.6	Separation of Azeotropic Mixtures in Sequence of Columns with	-
		Recycles at $R = \infty$ and $N = \infty$	71
	3.7	Nonsingularity of Separation Products Compositions at $R = \infty$	
		and $N = \infty$	72
	3.8	Conclusion	73
	3.9 3.10	Questions Exercises with Software	74 74
		References	75
4.			77
4.	-	tories of Thermodynamically Reversible Distillation Introduction	77
		Essence of Reversible Distillation Process and Its Peculiarities	78
		. Essence of Reversible Distillation Process	78
		2. Location of Reversible Distillation Trajectories	79
	4.2.3	•	
		Mixtures	80



Contents	ix
4.2.4. Column Sequence of Ideal Mixtures Reversible Distillation	81
4.2.5. Main Peculiarities of Reversible Distillation Column	82
4.3 Trajectory Bundles of Sharp Reversible Distillation	83
4.3.1. Bundles and Regions of Sharp Reversible Distillation	83
4.3.2. Condition in Tear-Off Points of the Reversible Distillation	
Trajectories	86
4.3.3. Possible Product Composition Regions	87
4.3.4. Necessary Condition of Sharp Reversible Distillation	88
4.3.5. Liquid and Vapor Flow Rates Changing along the Reversible	
Distillation Trajectories	89
4.4 Diagrams of Three-Component Mixture Reversible Distillation	92
4.4.1. Calculation of Reversible Distillation Trajectories	92
4.4.2. Scanning the Sides of the Concentration Triangle	93
4.5 Trajectories Bundles of Reversible Distillation for	
Multicomponent Mixtures	93
4.6 Diagrams of Extractive Reversible Distillation for	
Three-Component Mixtures	97
4.6.1. Condition in Tear-Off Points of the Extractive Reversible	
Distillation Trajectories	97
4.6.2. Azeotropic Mixtures	99
4.7 Trajectory Bundles of Extractive Reversible Distillation for	
Multicomponent Mixtures	100
4.8 Boundaries of Nonsharp Reversible Distillation	102
4.8.1. Three-Component Azeotropic Mixtures	102
4.8.2. Four-Component Azeotropic Mixtures	105
4.9 Conclusion	105
4.10 Questions	105
4.11 Exercises with Software	106
References	106
Distillation Trajectories and Conditions of Mixture Separability in	
Simple Infinite Columns at Finite Reflux	108
5.1 Introduction	108
5.2 Calculation of Distillation at Minimum Reflux for Ideal Mixtures	111
5.2.1. Underwood System of Equations	112
5.2.2. Evolution of Separation Product Compositions of	
One-Section Columns at Set Feed Composition	114
5.2.3. Evolution of Separation Product Compositions of	
Two-Section Columns at Set Feed Composition	117
5.3 Trajectory Tear-Off Theory and Necessary Conditions of	
Mixture Separability	120
5.3.1. Conditions of Distillation Trajectory Tear-Off at Sharp Splits	120
5.3.2. Trajectory Tear-Off Regions and Sharp Distillation Regions	123
5.3.3. Necessary Condition of Mixture Separability for the Set Split	124
5.4 Structure and Evolution of Section Trajectory Bundles for	
Three-Component Mixtures	126
5.4.1. The Product Is a Pure Component $(k = 1)$	126
5.4.2. The Product Is a Binary Mixture $(k = 2)$	129
5.4.3. The Product Is a Three-Component Mixture $(k = 3)$	136
5.4.4. The Product Is Azeotrope	140

5.



x Contents

	5.5	Structure and Evolution of Section Trajectory Bundles for	
		Four- and Multicomponent Mixtures	141
	5.5.	1. Four-Component Mixture	141
		2. Mixtures with Any Number of Components	147
	5.6	Conditions of Section Trajectories Joining and Methods of	
		Minimum Reflux Calculating	150
	5.6	Two Models of Feed Tray	150
		2. Conditions of Section Trajectories Joining	151
		3. Direct and Indirect Splits (One of the Products Is Pure	131
	5.0.	Component or Azeotrope)	152
	5.6	* * /	154
		4. Intermediate Splits5. Splits with Distributed Component	154
		i i	161
		6. Equations of Thermal Balance	
		7. Visualization of Section Trajectories	162
	5.7	Necessary and Sufficient Conditions of Separability	1.00
		of Mixtures	162
		1. Adiabatic Columns	162
		2. Nonadiabatic Columns	163
	5.8	Conclusion	164
	5.9		165
	5.10	Exercises with Software	166
		References	166
6.	Distil	lation Trajectories in Infinite Complex Columns	
		Complexes	170
	6.1	•	170
	6.2	Columns with Intermediate Inputs and Outputs of Heat:	
		"Pinch Method"	172
	6.3	Distillation Trajectories and Minimum Reflux Mode in Two-Feed	
		Columns with Nonsharp Separation in Intermediate Section	174
	63	Location of Reversible Distillation Trajectories of	
	0.0.	Intermediate Sections	175
	63	2. The Structure of Trajectory Bundles of Intermediate Sections	177
		3. Control Feed at Minimum Reflux Mode	178
		4. General Algorithm of Calculation of Minimum Reflux Mode	179
	6.4	Trajectories of Intermediate Sections of Extractive Distillation	1//
	0.4	Columns	181
	6.4	Sharp Extractive Distillation of Three-Component Mixtures	181
		2. Sharp Extractive Distillation of Four- and Multicomponent	101
	0.4.	Mixtures	186
	6.5	Conditions of Separability in Extractive Distillation Columns and	100
	0.5	Minimum Reflux Mode	187
	6.5		
	6.5.	1 2	187
	6.5.	1	188
	6.5.		190
	6.6	Determination of Minimum Flow Rate of Entrainer	193
	6.7	Distillation Complexes with Thermal Coupling Flows	195
	/-	1 IV 1 (D' ('11 1' C 1 '4 PP 1C 1'	
	6.7.	1. Kinds of Distillation Complexes with Thermal Coupling Flows	195



	Contents	XI
	6.7.2. Petlyuk Columns	197
	6.8 Calculation of Minimum Reflux Mode for Distillation Complexes	
	with Thermal Coupling Flows	200
	6.8.1. The Columns with Side Withdrawals of Flows	200
	6.8.2. The Columns with Side Strippings	202
	6.8.3. The Petlyuk Columns	204
	6.9 Distillation Trajectories in Complexes of Heteroazeotropic and	
	Heteroextractive Distillation	206
	6.9.1. Heteroazeotropic Distillation	207
	6.9.2. Heteroextractive Distillation	210
	6.10 Conclusion	212
	6.11 Questions	213
	References	213
7 .	Trajectories of the Finite Columns and Their Design Calculation	218
	7.1 Introduction	218
	7.2 Distillation Trajectories of Finite Columns: Possible	
	Compositions in Feed Cross Section	220
	7.2.1. Location of Section Trajectories	220
	7.2.2. Possible Compositions in Feed Cross Section	223
	7.3 Design Calculation of Two-Section Columns	226
	7.3.1. Direct and Indirect Splits of Mixtures with Any Number of	22/
	Components	226
	7.3.2. Intermediate Splits of Mixtures with Any Number of	227
	Components 7.2.2 Splits with a Distributed Component	227 239
	7.3.3. Splits with a Distributed Component7.3.4. Splits with Several Distributed Components: Preferred Split	242
	7.3.4. Spirts with Several Distributed Components. Treferred Spirt 7.3.5. Advantages of New Design Algorithms	243
	7.3.3. Advantages of New Design Algorithms 7.4 Design Calculation of Extractive Distillation Columns	243
	7.4.1. Three-Component Azeotropic Mixtures	245
	7.4.2. The Multicomponent Mixtures: The Top Product and the	213
	Entrainer Are Pure Components ($m_r = 1, m_e = 2$)	246
	7.4.3. The Multicomponent Mixtures: The Top Product Is a Binary	
	Mixture, the Entrainer Is a Pure Component $(m_r = 2, m_e > 2)$	247
	7.4.4. The Multicomponent Mixtures: The Top Product Is a Pure	
	Component, the Entrainer Is a Mixture $(m_r = 1, m_e > 2)$	247
	7.5 Design Calculation of "Petlyuk Columns" and of Columns with	
	Side Sections	249
	7.5.1. Design Calculation of "Petlyuk Columns"	249
	7.5.2. Design Calculation of Columns with Side Sections	252
	7.6 Determination of Necessary Tray Numbers at Heteroazeotropic	
	and Heteroextractive Distillation	255
	7.7 Conclusion	257
	7.8 Questions	259
	7.9 Exercises with Software	259
	References	260
8.	Synthesis of Separation Flowsheets	263
	8.1 Introduction	263
	8.2 Zeotropic Mixtures	265



xii Contents

8.2.1. Heuristic Rules of Synthesis	265
8.2.2. Estimation of the Expenditures on Separation	265
8.2.3. Preferability Regions for Ternary Mixtures	267
8.2.4. Systematic Identification of Alternative Sequences	269
8.2.5. Examples of Synthesis of Separation Flowsheets	271
8.3 Thermodynamically Improved and Thermally Integrated	
Separation Flowsheets	276
8.3.1. Thermodynamic Losses and Their Decrease	276
8.3.2. Thermally Integrated Separation Flowsheets	279
8.3.3. The Heat Pump	279
8.4 Multicomponent Azeotropic Mixtures: Presynthesis	281
8.4.1. Possible Product Segments at the Edges of Concentration	
Simplex	282
8.4.2. Possible Product Regions at the Boundary Elements of	
Concentration Simplex	283
8.4.3. Possible Sharp Splits in Columns with One Feed	286
8.4.4. Possible Sharp Splits in Columns with Two Feeds	287
8.4.5. The Most Interesting Splits of Columns with Decanters	288
8.4.6. Examples of Presynthesis	288
8.4.6.1. Example 1: Simple Columns	288
8.4.6.2. Example 1: Extractive Distillation	290
8.4.6.3. Example 2: Simple Columns	292
8.4.6.4. Example 2: Extractive Distillation	299
8.5 Multicomponent Azeotropic Mixtures: Automatic Sequencing	
and Selection	300
8.5.1. Selection of Splits	301
8.5.2. Examples of Sequencing and Selection	303
8.5.2.1. Example 1	303
8.5.2.2. Example 2	305
8.6 Binary and Three-Component Azeotropic Mixtures	307
8.6.1. Application of Semisharp Extractive Distillation	307
8.6.2. Application of Pressure Change	308
8.6.3. Choice of Entrainers	309
8.7 Petroleum Mixtures	312
8.7.1. Peculiarities of Petroleum as Raw Material for Separation	312
8.7.2. Methods of Petroleum Separability Increase	312
8.7.3. The Best Distillation Complex for Petroleum Refining	313
8.7.4. Main Succession of Petroleum Refining	314
8.7.5. Modernization of Units for Petroleum Refining	317
8.8 Conclusion	318
8.9 Questions	319
References	320
Short Glossary	325
Index	329



Preface

This book is devoted to distillation theory and its application. Distillation is the most universal separation technique. Industrial distillation consumes a considerable part of the world power output. The distillation theory enables one to minimize power and capital costs and thus opens up new ways of designing economical separation units. The most important constituent of the distillation theory is the geometric approach, which reveals general rules governing the variation of component concentrations along the distillation column. In other words, it provides general rules for the arrangement of distillation trajectories in the so-called concentration space, in which every point represents some mixture composition. A considerable part of the book is concerned with these general rules, which are used as the basis in developing new methods and algorithms for the optimal design of separation units.

The geometric approach to distillation was put forward by the German scientists Ostwald and Schreinemakers in the early twentieth century. During the years that followed, it has been developed by scientists from various countries. However, until recently, the geometric approach found little use in the design of distillation units. The progress in this field was made by developing the pure computational approach, more specifically, ways of describing the liquid-vapor equilibrium and algorithms for solving sets of distillation equations. This approach has been fruitful: it has resulted in universal computer programs that enable one to design a distillation column (system) of any type for separation of any kind of mixture. However, the pure computational approach gives no answer to a number of fundamental questions that arise in the optimal design of distillation processes, particularly in the case of azeotropic distillation. These questions are the following: (1) What are the feasible separation products for a given mixture? In other words, what components can be present in or absent from the separation products? (2) What minimum power is required to separate a given mixture into the desired components? (3) What minimum number of trays is necessary to separate a given mixture into the desired components at a fixed-power input? Answers to these questions have been provided only by a general geometric theory of distillation.

xiii



xiv Preface

Until recently, this theory had not advanced to a sufficient extent. Solutions were only obtained for particular cases. For many years, the author and his colleagues, relying on the results obtained by other researchers, have been putting a great deal of effort into elaborating general methods of the geometric theory to answer the fundamental questions listed above. An analysis of thermodynamically reversible distillation, the conception of "sharp" separation, the formulation of conditions under which distillation trajectories can tear-off from the boundaries of the concentration simplex, and the conditions of joining of column section trajectories have been particularly important steps in constructing the geometric theory of distillation. We have proposed a clear multidimensional geometric representation of distillation, which is valid for all types of distillation columns and complexes, for mixtures of any number of components and azeotropes, and for all splits. This representation provided answers to all the fundamental questions, which were previously enumerated. This success encouraged the author to write the present book.

The optimal design of a distillation plant includes the optimization of the sequence of the most economic columns and complexes for separation for a given mixture (flowsheet synthesis) and optimization of the operating and design parameters of these columns and complexes (optimal design calculations). Methods of the general geometric theory of distillation, encoded in software, provide quick and reliable solutions to both problems. The creation of this book necessitated the development of DistillDesigner software that allowed us to refine, check, and confirm the algorithms of optimal designing and also to provide for a significant portion of illustrations and exercises. The problems are solved neither by conventional "blind" methods nor by trial-and-error methods based on the designer's intuition. They are solved in a systematic way, and the solution has a geometric image so the designer can see that it is really optimal. The creation of the software product led, in its turn, to a revision of the general statements of the geometric distillation theory.

Furthermore, the book considers problems that are beyond the framework of the geometric theory of distillation but are still of importance from both the theoretical and practical standpoints.

Among these problems is the problem of maximizing energy savings by optimizing the type of separation unit and by maximizing heat recovery and the problem of the maximum yield of the most valuable products in the separation of thermolabile mixtures (e.g., the maximum yield of the light product in oil refining). Application of optimal design methods based on the general geometric theory of distillation and use of new, most economic distillation units and separation sequences bring the practice of separation to a much higher level.

This book is intended for a wide variety of specialists in the design and operation of separation units in the chemical, pharmaceutical, food, wood, petrochemical, oil-refining, and natural gas industries, and for those engaged in creating software for separation unit design. The circle of these specialists comprises software engineers, process designers, and industrial engineers. The software engineer will find new computational algorithms, the process designer will be provided with a useful



Preface xv

guide in his or her search for economic engineering solutions, and the industrial engineer will find ways of reducing the process cost. This book can serve as a manual for students and postgraduates who want to refine their understanding of distillation.

The book has many illustrations, without which understanding of the geometric theory would be impossible. The visualization of trajectory location in the concentration space has great practical significance, as it allows the process designer to understand the main peculiarities of separation of each particular mixture. Developing the geometric theory of distillation necessitated the introduction of some new terms. Furthermore, for some concepts, there are no unique, commonly accepted terms. For these reasons, the book is supplemented with a short glossary, which is believed to be useful for the reader. For better understanding of the subject, each chapter has an introduction that presents the problems to be considered, their brief history, and a conclusion, which summarizes the basic results. Besides that, each chapter contains questions for review and exercises with DistillDesigner software. The most important chapter for understanding the geometric theory of distillation is Chapter 5. The chapters preceding it are basically introductory, and those that follow speak mostly of the application of the theory.



Acknowledgments

The author is grateful to many people who have favored the creation of this book.

First, I express my gratitude to my closest assistant Roman Danilov whose participation was really indispensable. Together with him, I have developed the hitherto unrivaled software package that made it possible to check and put into practice the main ideas of this book. He also designed all the illustrations without which the book would not be comprehensible.

My debt of gratitude is to colleagues and research students who have taken part in numerous projects for decades: Victoria Avetyan, Vyacheslav Kiyevskiy, Maya Yampolskaya, Valentina Mashkova, Galina Inyayeva, Elizaveta Vinogradova, Zhanna Bril, Boris Isayev, Alexander Shafir, and Oleg Karpilovskiy.

My encounter with Professor Vladimir Platonov gave rise to my interest in distillation. Later acquaintance with Professor Leonid Serafimov led me to the investigation of the most complicated problems concerning azeotropic mixtures.

A number of scientists approved of my working on the book and favored it. I am grateful to Valeriy Kiva, Sigourd Skogestad, Arthur Westerberg, and Nikolay Kulov.

I am grateful to Andry Kalinenko and Vyacheslav Kiyevskiy, chiefs of the engineering firm ECT Service, where I have been working for a long time, for providing me with much support in developing new methods and writing this book.

I express my gratitude to Norsk University of Science and Technology for helping me when I was starting this book.

And I am thankful to my wife who made every effort so that my work would go on.

xvii



Nomenclature

A	separation work
A	stationary point of bond chain
A	vertex of product simplex
B	bottom stream (flow rate), kmol/sec
$C^{(k)}$	<i>k</i> -component boundary element of concentration simplex
C_n	concentration simplex for <i>n</i> -component mixture
d	dimension of trajectory bundle
D	overhead stream (flow rate), kmol/sec
E	entrainer stream (flow rate), kmol/sec
F	feed stream (flow rate), kmol/sec
h	enthalpy of liquid, kJ/kg or kcal/kg
H	enthalpy of vapor, kJ/kg or kcal/kg
h	heave key component
$i_D:i_B$	split in column (i_D and i_B – components of overhead and bottom products respectively)
i:j	split in section (<i>i</i> and <i>j</i> present and absent component of section product or pseudoproduct respectively)
K	equilibrium ratio
k	number of product components at sharp distillation
k	key component
k	key stationary point (pseudocomponent)
$K_j^{\infty} \ K^t$	equilibrium ratio of component j at infinite dilution
K^t	equilibrium ratio in tear-off point
l	light key component
L	liquid stream (flow rate), kmol/sec
m	number of product components at sharp distillation

xix



xx Nomenclature

m	number of stationary points of bond chain
n	number of components in a mixture
N	number of equilibrium stages
N^+ or N^-	stable or unstable node respectively
N_D^+ or N_D^-	stable or unstable node of overhead boundary
	element of concentration simplex or of
	distillation region respectively
N_B^+ or N_B^-	stable or unstable node of bottom boundary
	element of concentration simplex or of
	distillation region respectively
N_r^+ or N_r^-	stable or unstable node of rectifying trajectory
	bundle respectively
$N_{\scriptscriptstyle S}^+$ or $N_{\scriptscriptstyle S}^-$	stable or unstable node of stripping trajectory
	bundle respectively
N_e^+ or N_e^-	stable or unstable node of extractive trajectory
c c	bundle respectively
P	pressure, Pa
q	fraction of liquid in feed
Q	heat flow rate, kJ/sec or kcal/sec
qS	quasisaddle
R	reflux ratio
R_{\min}	minimum reflux ratio
$R_{\rm lim}^1$ or $R_{\rm lim}^2$	first or second boundary minimum reflux ratio
	respectively
R_{\min}^t or R_{\max}^t	minimum or maximum reflux ratio for trajectory
_	tear-off respectively
\mathop{Reg}_{ijk}	region
Regard	component order region
$\operatorname{Reg}_{D}^{(k)}$ or $\operatorname{Reg}_{B}^{(k)}$ or $\operatorname{Reg}_{D,E}^{(k)}$	k-component possible overhead or bottom or
	overhead-entrainer product region respectively
Reg_D or Reg_B or $\operatorname{Reg}_{D,E}$	<i>i</i> -present components and <i>j</i> -absent components
i i	possible overhead or bottom or overhead-
j j	entrainer product region respectively
$\operatorname{Reg}_{bound,D}^{j}$ or $\operatorname{Reg}_{bound,B}^{j}$	boundary of possible overhead or
or $\operatorname{Reg}_{bound,D,E}^{I}$	bottom or overhead-entrainer product region
i	respectively, <i>i</i> -present components, and <i>j</i> -absent
	components
$\operatorname{Reg}_r^{t(k)}$ or $\operatorname{Reg}_s^{t(k)}$ or $\operatorname{Reg}_e^{t(k)}$	<i>k</i> -component tear-off region of rectifying or
<i>z, z</i>	stripping or extractive section respectively
Reg^∞	distillation region at infinite reflux
$\operatorname{Reg}_{bound,D}^{\infty}, \operatorname{Reg}_{bound,B}^{\infty}$	top or bottom boundary element of distillation
	region at infinite reflux respectively
$\operatorname{Reg}^{\min,R}_{sep,r},\operatorname{Reg}^{\min,R}_{sep,s}$	separatrix min-reflux region for rectifying or
***	stripping section for given reflux R respectively



Nomenclature xxi

$\operatorname{Reg}_{sep,r}^{sh,R}, \operatorname{Reg}_{sep,s}^{sh,R}$	separatrix sharp split region for rectifying or stripping section for given reflux <i>R</i> respectively
$\operatorname{Reg}_{w,r}^R, \operatorname{Reg}_{w,s}^R \operatorname{Reg}_{w,e}^R$	rectifying or stripping or extractive section working region at given reflux <i>R</i> respectively
$\operatorname{Reg}_{sh,r}^{i:j}, \operatorname{Reg}_{sh,s}^{i:j}, \operatorname{Reg}_{sh,e}^{i:j(E)}$	sharp split region for rectifying or stripping or extractive section for split $i:j$ respectively
$\operatorname{Reg}_{rev,r}^h, \operatorname{Reg}_{rev,s}^l, \operatorname{Reg}_{rev,e}^m$	reversible distillation region for rectifying section with <i>h</i> heavy component or stripping section with <i>l</i> light component or extractive section with <i>m</i> middle component respectively
Reg _{att}	attraction region
	two liquid phases region
Reg_{L-L}	
$\operatorname{Reg}_{pitch}$	region of pitchfork
Reg _{simp}	product simplex at infinite reflux
Reg_{sub}	subregion of distillation at infinite reflux
Reg _{tang}	tangential pinch region
S	reboil ratio
S	entropy
S	saddle
S^1	tear-off point of section trajectory at sharp split
S^2	tear-off point of section trajectory at minimum reflux
$S^1 - S^2 - N^+$	boundary element of trajectory bundle at sharp split
$S^2 - N^+$	boundary element of trajectory bundle at minimum reflux
SN	saddle-node
S_r or S_s or S_m	saddle point of rectifying or stripping or
	intermediate trajectory bundle respectively
T	temperature, K
V	vapor stream (flow rate), kmol/sec
X	mole fraction of liquid phase
x_{rev}^t	tear-off point of reversible distillation
TEV	trajectory
$\chi'_{\mathcal{D}}$	pseudoproduct point
x_D' x_f^{∞} or x_f^{\min}	composition on first plate under feed cross section
,,	at which number of stripping section plate is infinite or minimal respectively
x_{f-1}^{∞} or x_{f-1}^{\min}	composition on first plate above feed cross section at which number of rectifying section plate is infinite or minimal respectively
x_{rev}^{branch}	branch point of reversible distillation trajectory
(x_f^{sh}) or (x_{f-1}^{sh})	composition on first plate under or above feed
· / · · / -1/	cross section at sharp split respectively

cross section at sharp split respectively



xxii Nomenclature

ε

$\begin{bmatrix} x_f^{sh} \end{bmatrix}$ or $\begin{bmatrix} x_{f-1}^{sh} \end{bmatrix}$	composition segment on first plate under or above
,	feed cross section at sharp split respectively
y	mole fraction of vapor phase
z	mole fraction of liquid-vapor mixture
1, 2, 3	components 1, 2, 3 respectively
1, 2; 1,3	mixtures of components 1 and 2; 1 and
	3respectively
1-2, 1-2-3	boundary elements of concentration simplex
12, 13	binary azeotropes of components 1 and 2; 1 and
	3respectively
123, 124	ternary azeotropes of components 1, 2, and 3;
	1, 2, and 4 respectively
123, 132	regions of component order

Greek and Other Symbols

component recovery

difference eigenvalue of distillation matrix excess reflux factor infinity
excess reflux factor
infinity
relative volatility
sum
the root of an Underwood equation for both sections
the root of an Underwood equation for rectifying or stripping section
product purity
thermodynamic efficiency
composition interval on plate under or above feed cross section
volatility of component 1 relative of component 2, of component 3
distillation bundle included stationary points N^- , S , N^+
mixing in feed cross section
bond, trajectory of distillation, one-dimensional trajectory bundle
set of all bonds (or of all distillation trajectories) of distillation bundle
flows between sections of distillation complex
decanter

Subscripts and Superscripts

az	azeotrop
ad	adiabatic



> **Nomenclature** xxiii В bottom product con condenser D overhead product component of entrainer e Eentrainer first plate under entrainer cross section e. e-1 first plate above entrainer cross section feed first plate under feed cross section f-1 first plate above feed cross section h heave key component h Haz. heteroazeotrop component of mixture i. Dcomponent i, which is present in product D imp intermediate condenser or reboiler int irr irreversible component j, which is absent on the boundary element of concentration simplex j, DEcomponent j, which is absent in product D and entrainer Eplate of column stationary point kcomponent of mixture k plate of column key component kev light key component of mixture L1, L2 first, second liquid phases intermediate product Mintermediate section m middle volatility component of mixture m new value at iterations new old value at iterations oldpinch pinch pr preferable rectifying reboiler reb rev reversible stripping stationary point st tear-off point first and second tear-off points of reversible distillation *t*1, *t*2 trajectories respectively (*k*) k-component boundary element of concentration simplex, k-component point, product point with k product components



xxiv Nomenclature

w working region, working trajectory1,2,3...; feed 1,2; variant 1,2,3; column1,2,3...respectively

Nomenclature to Figures

A endpoint of tear-off segment of distillation

trajectories

 $A_1, A_2, A_3 \dots$ vertexes of possible product composition regions

Az azeotropes

boxed digits component order regions

C-1, *C*-2... columns

dash-dotted line line of material balance

dashes tray compositions on composition profiles

dotted line trajectory of reversible distillation

dotty line separatrix

double segment possible composition of overhead product or

trajectory tear-off segment of top section

thick black segment possible composition of bottom product or

trajectory tear-off segment of bottom section

gray segment tear-off segment of extractive distillation

trajectories

F + E composition point of feed and entrainer mixture

 F_0 composition point of initial feed

 $F_1 + F_2$ composition point of mixture of feeds F_1 and F_2

H height of column
HD heave diesel oil
HN heave naphta
LD light diesel fuel
LN light naphta

little black or white circle stable or unstable node of concentration simplex

respectively

little cross circle saddle of concentration simplex little cross square bottom composition point little square overhead composition point feed composition point short segment with arrow tie-line liquid-vapor

st steam

thick line trajectory of distillation thin line equivolatility line

(1), (2)... column (1) or (2) respectively (1), (2)... split (1) or (2) respectively

 $\alpha_{12}, \alpha_{13}...$ equivolatility line of components 1 and 2, 1 and

3...respectively