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978-0-521-17222-6 - The Integration of Functions of A Single Variable, Second Edition

G. H. Hardy

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