## THE MECHANICS OF THE CIRCULATION

### SECOND EDITION

Continuing demand for this book confirms that it remains relevant over 30 years after its first publication. The fundamental explanations are largely unchanged, but in the introduction to this second edition the authors are on hand to guide the reader through major advances of the last three decades.

With an emphasis on physical explanation rather than equations, Part I clearly presents the background mechanics. The second part applies mechanical reasoning to the component parts of the circulation: blood, the heart, the systemic arteries, microcirculation, veins and the pulmonary circulation. Each section demonstrates how an understanding of basic mechanics enhances our understanding of the function of the circulation as a whole.

This classic book is of value to students, researchers and practitioners in bioengineering, physiology and human and veterinary medicine, particularly those working in the cardiovascular field, and to engineers and physical scientists with multidisciplinary interests.

"... essential reading for anyone who is interested in the mechanics of the circulation. The normally incomprehensible mechanical laws are explained so clearly that even the non-mathematically minded will have no difficulty, which makes me very sorry that it was not available when I was grappling with these problems."

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'Here is a book on the mechanics of the circulation that is equally accessible to those trained in the life sciences and in the mechanical sciences.'

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# THE MECHANICS OF THE CIRCULATION

## SECOND EDITION

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With the Assistance of

K.H. PARKER Imperial College



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## Contents

| Foreword<br>Preface to the First Edition<br>Acknowledgements |  | <i>page</i> xiii |      |
|--|--|------------------|------|
|  |  | xvii<br>xx       |      |
|  |  |                  | Intr |
|  | Part I Background mechanics                      | 1                |      |
| 1  | Particles and continuous materials               | 3                |      |
| 2  | Particle mechanics                               | 7                |      |
|  | Position   | 7                |      |
|  | Velocity   | 8                |      |
|  | Acceleration                                     | 12               |      |
|  | Newton's laws of motion: mass and force          | 14               |      |
|  | Momentum   | 20               |      |
|  | Work and energy                                  | 20               |      |
| 3  | Units  | 24               |      |
|  | The difference between units and dimensions      | 24               |      |
|  | Mass, length, and time as fundamental units      | 25               |      |
|  | The inconvenience of force as a fundamental unit | 26               |      |
|  | Energy and heat                                  | 27               |      |
|  | The concept of substance                         | 27               |      |
|  | Dimensional homogeneity and consistency of units | 27               |      |
|  | The use of volume and flow rate in physiology    | 27               |      |
|  | Système International (SI)                       | 28               |      |
| 4  | Basic ideas in fluid mechanics                   | 31               |      |
|  | Stress   | 31               |      |
|  | Hydrostatic pressure                             | 33               |      |
|  | Stress in a moving fluid: viscosity              | 35               |      |
|  | The equation of motion of a fluid                | 38               |      |

| Cambridge University Press   |
|--|
| 978-0-521-15177-1 — The Mechanics of the Circulation                           |
| C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker |
| Frontmatter  |
| More Information   |

| vi | Contents  |            |
|----|---|------------|
|    | Convective and local acceleration                                 | 40         |
|    | Conservation of mass  | 41         |
|    | Bernoulli's theorem   | 42         |
| 5  | Flow in pipes and around objects                                  | 45         |
|    | Poiseuille flow in a tube   | 45         |
|    | Flow in the entrance region                                       | 50         |
|    | The idea of the boundary layer                                    | 52         |
|    | Reynolds number   | 55         |
|    | Turbulence in pipe flow   | 56         |
|    | Unsteady flow in a very long pipe                                 | 58         |
|    | Effects of constrictions on pipe flow characteristics             | 61         |
|    | Flow in curved pipes  | 66         |
|    | Flow past bodies  | 69         |
| 6  | Dimensional analysis  | 80         |
|    | Similarity and the idea of scale models                           | 81         |
|    | Some examples of scaling in biological systems                    | 81         |
|    | A method of obtaining homogeneous relationships between variables | 82         |
| 7  | Solid mechanics and the properties of blood vessel walls          | 86         |
|    | Definitions of elastic properties                                 | 86         |
|    | The properties of blood vessel walls                              | 91         |
|    | Statics of an elastic tube  | 100        |
| 8  | Oscillations and waves  | 105        |
|    | Simple harmonic motion  | 105        |
|    | Simple waves  | 112        |
|    | Damping   | 116        |
|    | Wave reflections and resonance                                    | 120        |
|    | Linearity   | 123        |
|    | Fourier analysis  | 126        |
| 9  | An introduction to mass transfer                                  | 128        |
|    | Diffusion   | 129        |
|    | The colloidal state   | 133        |
|    | Mass transfer coefficients  | 133        |
|    | Diffusion through pores and membranes                             | 135        |
|    | Restricted diffusion  | 136<br>137 |
|    | Active transport  |            |
|    | Permeability<br>Filtration through membranes                      | 138<br>138 |
|    | Osmosis   | 138        |
|    | A simple mass transfer model                                      | 139        |
|    | r ompre muss transfer moder                                       | 1 - 1      |

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|--|
| 978-0-521-15177-1 — The Mechanics of the Circulation                           |
| C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker |
| Frontmatter  |
| More Information   |

|    | Contents  | vii |
|----|---|-----|
|    | The interaction of bulk flow and diffusion      | 142 |
|    | The Schmidt number                              | 145 |
|    |   |     |
|    | Part II Mechanics of the circulation            | 147 |
| 10 | Blood   | 149 |
|    | Viscosity of fluids and suspensions             | 149 |
|    | Spherical particles                             | 151 |
|    | Asymmetric particles                            | 154 |
|    | Viscosity of plasma                             | 155 |
|    | Osmotic pressure of plasma                      | 156 |
|    | The suspended elements                          | 157 |
|    | The blood cells                                 | 157 |
|    | Red cells                                       | 158 |
|    | White cells                                     | 165 |
|    | Platelets                                       | 165 |
|    | Blood coagulation                               | 167 |
|    | Thrombosis                                      | 168 |
|    | Mechanical properties of whole blood            | 169 |
|    | Sedimentation of red cells                      | 170 |
|    | Principles of measurement of blood viscosity    | 171 |
|    | Viscous properties of blood                     | 174 |
| 11 | The heart                                       | 178 |
|    | Anatomy of the heart                            | 179 |
|    | The cardiac cycle                               | 183 |
|    | Electrical events                               | 183 |
|    | Mechanical events                               | 184 |
|    | Properties of cardiac muscle                    | 186 |
|    | Structure                                       | 186 |
|    | Static mechanical properties of cardiac muscle  | 189 |
|    | Dynamic mechanical properties of cardiac muscle | 191 |
|    | Summary   | 201 |
|    | Mechanical behaviour of the intact heart        | 202 |
|    | Left ventricular shape and wall stresses        | 204 |
|    | Right ventricular shape                         | 209 |
|    | The mechanics of the entire ventricle           | 210 |
|    | Summary   | 224 |
|    | Fluid mechanical aspects of cardiac function    | 225 |
|    | Right heart                                     | 225 |
|    | Left heart                                      | 227 |
|    | Sounds and murmurs in the heart                 | 234 |

| viii | Contents  |     |
|------|---|-----|
|      | Sounds  | 234 |
|      | Murmurs   | 236 |
|      | Further reading   | 237 |
| 12   | The systemic arteries   | 238 |
|      | Anatomy and structure   | 239 |
|      | The anatomy of large blood vessels                              | 239 |
|      | Branching ratios and angles                                     | 241 |
|      | The structure of the arterial wall                              | 244 |
|      | Arterial wall thickness   | 250 |
|      | Changes in the arterial wall with age                           | 251 |
|      | Blood pressure and flow in systemic arteries                    | 255 |
|      | Transmural pressures  | 256 |
|      | Unsteady pressure in large arteries                             | 259 |
|      | Flow  | 262 |
|      | Terminology   | 265 |
|      | Fourier analysis  | 266 |
|      | Wave propagation in arteries                                    | 269 |
|      | The Windkessel model  | 270 |
|      | The propagation of the pressure wave                            | 271 |
|      | Determination of the wave speed                                 | 272 |
|      | Comparison of theory with experiment                            | 275 |
|      | Further limitations of the simple elastic model                 | 277 |
|      | Reflection and transmission of the wave at junctions            | 278 |
|      | Reflection at a single junction                                 | 278 |
|      | The matching of impedances                                      | 281 |
|      | Positive and negative reflection                                | 283 |
|      | Physiological evidence of wave reflections                      | 285 |
|      | Multiple reflections  | 288 |
|      | Interpretation of observed pressure waveforms in large arteries | 291 |
|      | The effect of taper   | 294 |
|      | The influence of nonlinearities                                 | 297 |
|      | Viscous effects   | 299 |
|      | Effect of blood viscosity on flow-rate waveform                 | 299 |
|      | Effect of viscosity on wave propagation                         | 301 |
|      | Effect of wall visco-elasticity                                 | 304 |
|      | Other types of wave   | 304 |
|      | Flow patterns in arteries                                       | 306 |
|      | Velocity profiles in large arteries                             | 306 |
|      | Physical mechanisms underlying the velocity profiles            | 313 |
|      | Stability and turbulence  | 321 |

Cambridge University Press 978-0-521-15177-1 — The Mechanics of the Circulation C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker Frontmatter <u>More Information</u>

|    | Contents  | ix  |
|----|---|-----|
|    | Mixing and mass transport in arteries                           | 328 |
|    | Mixing in the heart and large blood vessels                     | 328 |
|    | Mass transport across artery walls                              | 333 |
|    | Appendix: Impedance   | 338 |
|    | Further reading   | 341 |
| 13 | The systemic microcirculation                                   | 343 |
|    | The organization of a microvascular bed                         | 344 |
|    | The arteriolar system   | 344 |
|    | The capillary system  | 346 |
|    | The venular system  | 349 |
|    | The lymphatic system  | 350 |
|    | The structure of the vessels of the microcirculation            | 350 |
|    | The arterioles  | 351 |
|    | The capillaries   | 353 |
|    | The venules   | 358 |
|    | The lymphatics  | 360 |
|    | The junctions between vascular endothelial cells                | 360 |
|    | The pinocytic vesicles  | 363 |
|    | The interstitial space  | 363 |
|    | Static mechanical properties of the microcirculatory vessels    | 363 |
|    | Elastic properties of the arterioles                            | 364 |
|    | Mechanical properties of the capillaries                        | 366 |
|    | Elastic properties of the venules                               | 368 |
|    | Pressure in the microcirculation                                | 368 |
|    | The distribution of pressure                                    | 368 |
|    | The propagation of cardiac pressure oscillations                | 375 |
|    | Pressure in the interstitial space                              | 376 |
|    | Flow in models and in the large vessels of the microcirculation | 378 |
|    | The motion of single particles at very low flow rates           | 378 |
|    | The motion of single particles at high flow rates               | 381 |
|    | The motion of single red blood cells in Poiseuille flow         | 381 |
|    | The flow of concentrated suspensions of particles and red cells | 384 |
|    | The viscosity of whole blood                                    | 386 |
|    | Radial dispersion of red cells                                  | 387 |
|    | The cell-free layer   | 387 |
|    | Velocity profiles in vessels                                    | 391 |
|    | Blood flow in capillaries                                       | 392 |
|    | Positive clearance  | 394 |
|    | Negative clearance  | 396 |
|    | Mass transport in the microcirculation                          | 399 |

| Cambridge University Press   |
|--|
| 978-0-521-15177-1 — The Mechanics of the Circulation                           |
| C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker |
| Frontmatter  |
| More Information   |

| x  | Contents  |     |
|----|---|-----|
|    | Filtration and reabsorption of water within single capillaries            | 400 |
|    | Capillary pressure and filtration of water in whole organ<br>preparations | 405 |
|    | The dependence of plasma oncotic pressure on protein                      | 403 |
|    | concentration   | 407 |
|    | Evidence for the existence of filtration pores in the capillary wall      | 407 |
|    | Diffusion across the capillary wall                                       | 408 |
|    | Methods of measuring permeability coefficients                            | 410 |
|    | The diffusion pathway across the capillary wall                           | 417 |
|    | The Pappenheimer equivalent pore theory                                   | 418 |
|    | The pathway for water transport across the capillary wall                 | 419 |
|    | The transport of large molecules  | 420 |
|    | Further reading   | 424 |
| 14 | The systemic veins  | 426 |
|    | Anatomy   | 427 |
|    | Transmural pressure and static elastic properties                         | 429 |
|    | The resistance to bending of a tube wall                                  | 438 |
|    | Dynamics of blood flow in large veins                                     | 440 |
|    | Observed pressure and flow-rate waveforms                                 | 441 |
|    | Wave propagation in veins   | 443 |
|    | Flow patterns and velocity profiles in veins                              | 450 |
|    | Flow in collapsible tubes   | 451 |
|    | Model experiments   | 452 |
|    | Mechanisms  | 456 |
|    | Physiological evidence: Korotkoff sounds                                  | 459 |
|    | Mechanics of venous beds  | 460 |
|    | Elevation of a venous bed above the level of the heart                    | 461 |
|    | Contraction of skeletal muscle  | 461 |
|    | Respiratory manoeuvres  | 464 |
| 15 | The pulmonary circulation   | 467 |
|    | Anatomy   | 468 |
|    | Pulmonary circulation   | 468 |
|    | Bronchial circulation   | 475 |
|    | Transmural pressure and static elastic properties of vessels              | 475 |
|    | Intravascular pressure  | 476 |
|    | Perivascular pressure   | 476 |
|    | Elastic properties  | 480 |
|    | Pulmonary blood volume  | 482 |
|    | Dynamics of blood flow in large pulmonary vessels                         | 489 |
|    | Waveforms   | 489 |

Cambridge University Press 978-0-521-15177-1 — The Mechanics of the Circulation C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker Frontmatter <u>More Information</u>

| Contents                         | xi  |
|----------------------------------|-----|
| Wave propagation                 | 491 |
| Flow patterns                    | 494 |
| Pulmonary vascular resistance    | 494 |
| Flow in the alveolar sheet       | 494 |
| Zonal distribution of blood flow | 499 |
| Effect of lung mechanics         | 501 |
| Further reading                  | 504 |
| Index                            | 507 |
| Table I                          | 524 |

Cambridge University Press 978-0-521-15177-1 — The Mechanics of the Circulation C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker Frontmatter <u>More Information</u>

## Foreword

When I arrived at the Physiological Flow Studies Unit, Imperial College, in 1971, the writing of *The Mechanics of the Circulation* was already underway. The book had been commissioned by Oxford University Press to be delivered in 1972 and the Tuesday afternoon book meeting was a regular event. From the outset, the purpose of the book was seen as presenting cardiovascular mechanics in a rigorous but accessible way. It was not meant to be a textbook, but an introduction to the subject that would be useful to a wide range of readers from medical students to experts in either mechanics or cardiovascular physiology.

The Mechanics of the Circulation was finally published in 1978 and it was obvious that the authors had succeeded in their purpose. It was a truly interdisciplinary book, its authors having trained in medicine, mathematics and engineering, but there was a continuity of style and content that remains unusual in multidisciplinary, multi-author books. Individual authors wrote the first drafts of the different sections of the book closest to their expertise, but they all had an equal say in the final product which, as evidenced by the time it took to write the book and the heat that was generated in those weekly meetings, was no easy task.

The book had an enormous impact on the emerging field of cardiovascular mechanics and, by extension, on the development of the discipline of bioengineering as an essentially multidisciplinary field of study. It was reprinted and published as a paperback. Then, for reasons known only to the publisher, it was allowed to go out of print. In the years that followed there were occasional discussions about writing a second edition to incorporate the many advances that had taken place in the understanding of the cardiovascular system. But, because of other pressures and activities, the authors never found the time and the book became unavailable (except for the Russian and Chinese translations which continued to be available for several decades).

With the authors all retired, new discussions arose about a second edition and I was very honoured to be asked to be involved. We had many meetings about the changes that were needed and how the book could be made more relevant to the present time. It very quickly became evident, however, that the explosion of knowledge about the

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xiv

#### Foreword

physiology and mechanics of the cardiovascular system during the past 30 years made it impossible to embrace the whole subject in a single book. After much discussion, it was decided that the one thing that has remained constant over the years is the basic mechanics, which was the primary subject of the original book. We therefore decided to republish rather than rewrite the original book. This volume, with the addition of this foreword, a new preface, a few minor corrections and a greatly enhanced index, is the result.

Some flavour of the differences in research on the circulation between 1970 and 2010 can be gained simply by considering the way the old and the new versions of the book were produced. The original book was written in longhand and transcribed by a typist. Editing involved handwritten comments in the margins and the index involved annotated filing cards that were sorted by hand. The book was set by hand and the figures were reproduced using photolithography. The current book was prepared by scanning the original into a text file generated by an optical character recognition program. The text files were edited on a computer into a LaTeX file which generated the final format electronically. The output of the LaTeX program was edited via email and the new index was generated using the 'makeindex' function in LaTeX. Finally, a LaTeX-compatible printing press was used to convert the electronic form of the book into the printed hard copy. Every aspect of cardiovascular science has undergone a similar revolution.

In the compilation of a new, greatly expanded index for this volume, I have been struck by two things about *The Mechanics of the Circulation*: its completeness and its cohesiveness.

In the course of introducing the mechanics of the circulation, the book covers the anatomy and physiology of the circulation in considerable detail and even includes some examples of its pathology. There are, inevitably, some omissions. For instance, the extracellular material at the outer surface of endothelial cells receives only the most fleeting of mentions in Chapter 13 and is never named as the glycocalyx. And in the extensive discussion of waves in the circulation there is no mention of the water hammer equation that so conveniently relates changes in pressure and velocity. It is remarkable, however, how rare these omissions are given the breadth of material covered.

Even more impressive is the cohesiveness of the book. The authors have taken great care in the cross-referencing between the different sections. 'Part I: Background mechanics' provides a thorough grounding in basic mechanics, with extensive links to the application of these principles to the cardiovascular system. 'Part II: Mechanics of the circulation' deals with the different parts of the circulation in turn. Here the links are not only to the basic principles, but also to the other parts of the circulation with similar or opposing properties.

From my personal experience and from the experience of other colleagues working on the circulation, *The Mechanics of the Circulation* is a very valuable book. It Cambridge University Press 978-0-521-15177-1 — The Mechanics of the Circulation C. G. Caro, T. J. Pedley, R. C. Schroter, W. A. Seed, Assisted by K. H. Parker Frontmatter <u>More Information</u>

#### Foreword

XV

provides an introduction to mechanics for those trained in physiology, medicine and biology and an introduction to the anatomy and physiology of the circulation for those trained in mechanics, engineering and mathematics. Virtually everyone I know in the field has a well-thumbed copy on their bookshelf and many have used it as a basic text for both undergraduate and graduate courses.

Thirty years after its original publication, I am delighted that this classic book is once again being made available to experts and, most importantly, to students – the experts-to-be.

Kim H. Parker July 2010