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978-0-521-14927-3 — A Physical Introduction to Suspension Dynamics

Élisabeth Guazzelli , Jeffrey F. Morris , Illustrated by Sylvie Pic

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