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978-0-521-13408-8 - An Introduction to the Theory of Graph Spectra

Dragos Cvetkovic, Peter Rowlinson and Slobodan Simic

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