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978-0-521-12822-3 - Geometric Analysis of Hyperbolic Differential Equations: An Introduction

S. Alinhac

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