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978-0-521-11418-9 - The Theory of Finite Linear Spaces: Combinatorics of Points and Lines

Lynn Margaret Batten and Albrecht Beutelspacher

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