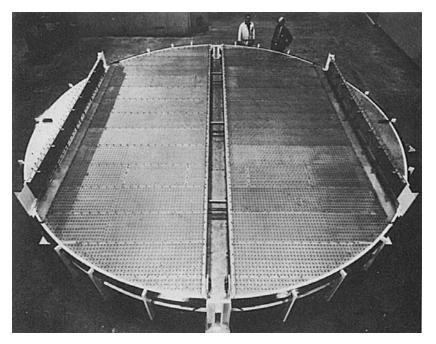


Distillation tray fundamentals





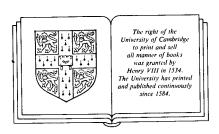
Trial assembly of large two-pass slotted sieve trays. (Courtesy of Union Carbide Corporation.)



# Distillation tray fundamentals

M.J.LOCKETT

Union Carbide Corporation



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## Preface

The design and performance of distillation trays is one of the most thoroughly studied topics in chemical engineering. Papers dealing with trays are available in abundance but the information they contain is often conflicting. Indeed, by searching hard enough it is usually possible to find some published information to support nearly any contention one cares to make about how trays work. One aim of this book has been to draw together and interpret much of this previous work.

It has not been my intention to write a design manual for tray design. Others have done this far more effectively than I, and some such sources are cited in Chapter 1. The approach I have taken is to assume that the reader is already familiar with elementary design methods as given in the standard undergraduate textbooks. What I have attempted is to delve a little deeper into the empirical correlations and equations which are used for tray design and to indicate their origins and shortcomings. The sequence of the material covered is such that, when coupled with the outline design procedure given in Chapter 1, it is relatively straightforward to adapt it to and improve existing design methods. Having said all that, I suppose this book was mainly written for the same reason that most books of its type are written – having worked in an area, in this case distillation trays, for some time with considerable enjoyment, it felt appropriate to convey my enthusiasm for the subject to others.

Distillation trays are seemingly so simple that it may be surprising that they warrant a whole book, albeit a small one, to themselves. Sieve tray decks are, after all, hardly more than sheets of metal with a few holes punched in them. This of course is part of the fascination – that the behaviour of something so simple can be so difficult to predict with regard to its hydrodynamic and mass transfer performance. Another equally intriguing aspect is the interplay between the topics covered in this book



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and the marketing and selling of trays. Distillation column internals are marketed very competitively as a glance at the advertisements in the popular chemical engineering magazines will testify. It is necessary to be aware that however erudite and interesting in their own right are theories of tray behaviour, they must in the end be translated into the design of pieces of metal which work reliably and at reasonable cost. Thus, those involved with trays span a wide range from those concerned solely with metal fabrication through to researchers into fairly esoteric irreversible thermodynamics. This complex mix of concerns and priorities also provides much of the subject's interest.

It is hoped that most people who deal with distillation trays at any level will find something of value in the pages that follow. However, the book is primarily aimed at the process engineer involved with design who wishes to know more than can be obtained by simply applying correlations. In addition, those concerned with specifying and buying trays should find it useful, as should those troubleshooting malfunctioning columns. I know from experience that it forms a reasonable basis for a graduate course, and the lack of answers to many of the questions posed should also provide a reasonable stimulus for research workers in this area of chemical engineering.

The book had its origins in a course of lectures I gave on distillation in the late 1970s to graduate students at the University of Manchester Institute of Science and Technology. When I was asked to give a course on distillation trays at the University of Aston to practising engineers as part of the continuing education series of the Institution of Chemical Engineers, the idea took hold of developing the material into a book. A further impetus was provided when I joined the Linde Division of Union Carbide, responsible for distillation engineering and development. This helped me put some of the more theoretical material into context as it impacts on the practising engineer.

Although the book was started while I was at UMIST, 95% of it was completed at nights and weekends while working for Union Carbide. In retrospect I doubt whether I would have started it if I had known it would be written outside the cloistered life of the university. In the event, my wife and children were extremely patient and understanding during its completion in spite of my absence from numerous school concerts, baseball games and skiing trips.

There are of course many other people to whom acknowledgement is due. In particular I would like to thank K E Porter who introduced me to the subject and taught me the importance of asking the right questions about research problems. I also appreciated working with the late G L



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Standart, who impressed on me the other aspect – the importance of giving the right answers! A source of inspiration has been the research students with whom I have had the good fortune to work over the years, and this book is built substantially on their efforts. Colleagues who have read the manuscript and contributed suggestions include M R Resetarits and D R Summers to whom thanks are also due, although errors and omissions are of course solely my own responsibility. Mrs Anita Strzalkowski did a sterling job of transforming my ill-written scrawl into a typewritten manuscript with good-humour and patience, and J D Augustyniak drew the figures with his usual skill and attention to detail. Finally I would like to thank the directors of Union Carbide for permission to publish the book.



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## Nomenclature

Unless otherwise stated locally, the units used are as given below. In particular, the following units should be used in equations which are not dimensionless. The nomenclature of the original sources has been retained as far as possible. The terms gas and vapour are used interchangeably.

- A Cross-sectional area, m<sup>2</sup>
- A Constant in eqn. (4.11)
- A Defined by eqn. (9.32)
- A<sub>b</sub> Tray bubbling area, m<sup>2</sup>
- A<sub>d</sub> Downcomer cross-sectional area, m<sup>2</sup>
- $A'_{da}$  Area under splash baffle, m<sup>2</sup>
- $A_h$  Area of holes in tray deck, m<sup>2</sup>
- A<sub>n</sub> Net area for liquid disengagement above tray, m<sup>2</sup>
- A<sub>sc</sub> Curtain area of 'closed' valves, m<sup>2</sup>
- Av Area of valve disk, m<sup>2</sup>
  - a Interfacial area per unit volume of two-phase dispersion, m<sup>2</sup> m<sup>-3</sup>
  - a Parameter describing jet shape, eqn. (2.17)
  - a Parameter in eqn. (2.31)
  - a Defined by eqns. (10.8)
  - a' Interfacial area per unit volume of vapour, m<sup>2</sup> m<sup>-3</sup>
  - $\bar{a}$  Interfacial area per unit volume of liquid, m<sup>2</sup> m<sup>-3</sup>
  - B Defined by eqns. (9.32)
- $B_s$  Oscillation number, eqn. (5.23)
- b Intercept of equilibrium line (binary)
- b Constant in eqn. (4.16)
- b Defined by eqns. (10.8)
- C Defined by eqn. (3.25)
- C Defined by eqn. (9.32)
- C<sub>d</sub> Discharge coefficient



```
Nomenclature
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      C<sub>0</sub> Drop drag coefficient
     CF
            Capacity factor based on A_b, m s<sup>-1</sup>
     CF'
            Capacity factor based on A_n, m s<sup>-1</sup>
    CF" Capacity factor from Fig. 5.1, m s<sup>-1</sup>
          Theoretical maximum capacity factor, eqn. (5.10), m s<sup>-1</sup>
  CF_{\max}
    CF<sub>0</sub> Capacity factor at zero liquid load, m s<sup>-1</sup>
       c Velocity of sound, m s<sup>-1</sup>
       D Column diameter, m
       D Defined by eqn. (9.32)
D_{\rm G}, D_{\rm L} Diffusion coefficient in vapour and liquid phase, m<sup>2</sup> s<sup>-1</sup>
      D<sub>L</sub> Diffusion coefficient in liquid phase at infinite dilution, m<sup>2</sup> s<sup>-1</sup>
      De Eddy diffusivity for liquid mixing, m<sup>2</sup> s<sup>-1</sup>
    De_G Eddy diffusivity for vapour mixing, m<sup>2</sup> s<sup>-1</sup>
      d<sub>b</sub> Bubble diameter, m
      d_{\rm bs} Sauter mean bubble diameter, m
      d_{\rm h} Hole diameter, m
           Jet diameter, m
           Drop diameter, m
      d_{\rm p}
           Mean drop diameter, m
     d_{\rm ps}
           Sauter mean projected drop diameter, m
           Diameter of drops in subgroup i, m
   d_{p}(j)
     E^+
           Liquid entrainment rate, kg-mol s<sup>-1</sup>
     E_{\rm H}
           Hausen tray efficiency
E_{\rm HL}, E_{\rm HV} Hausen liquid and vapour tray efficiency
     E_{\mathrm{m}}
           Liquid entrainment rate, kg s<sup>-1</sup>
   E_{\mathsf{ML}}
           Murphree liquid phase tray efficiency
           Murphree vapour phase tray efficiency
   E_{MV}
          Apparent Murphree vapour phase tray efficiency
   E_{MV}^{a}
           Vaporisation tray efficiency for component i on tray n
     E_{ni}^{\rm v}
     E_0
          Section efficiency
          Murphree vapour phase point efficiency
   E_{OG}
     E_{s}
          Standart material efficiency
          Standart enthalpy efficiency
    E_{\mathrm{SH}}
          Standart component efficiency
E_{\rm TL}, E_{\rm TV} Thermal efficiency in liquid and vapour phase
           Liquid entrainment rate \div vapour rate, (kg-mol s<sup>-1</sup>) \div (kg-mol s<sup>-1</sup>)
          Liquid entrainment rate \div vapour rate, (kg s^{-1}) \div (kg s^{-1})
         E^+/L_0
     e_0
      F Defined by eqn. (9.39)
   F(j) Number fraction of drops having size d_n(j)
          Hole F factor, u_h \rho_G^{0.5}, kg<sup>0.5</sup> m<sup>-0.5</sup> s<sup>-1</sup>
          Critical value of hole F factor
(F_h)_{crit}
```



Nomenclature xvii

- $F_R$  Reaction at the plate, N
- $F_s$  Superficial F factor,  $u_s \rho_G^{0.5}$ ,  $kg^{0.5} m^{-0.5} s^{-1}$
- F<sub>w</sub> Frictional force due to walls, N
- $F_r$  Force, N
- FF Flood factor or fractional approach to flooding
- FP Flow parameter, eqn. (1.1)
- Fr Froude number,  $u_s^2/gh_{cl}$
- Fr' Modified Froude number,  $Fr \rho_G/(\rho_L \rho_G)$
- $Fr_1$  Froude number for liquid flow,  $u_{L1}/(gh_1)^{0.5}$
- $Fr_h$  Froude number,  $u_h[\rho_G/gh_{cl}(\rho_L-\rho_G)]^{0.5}$
- f Friction factor for froth flow
- $f_i$  Fraction of vapour flow carried by bubbles of species i
- $\bar{f}_{ni}^{L}, \bar{f}_{ni}^{v}$  Fugacity of component i in liquid and vapour leaving tray n, bar
  - G Vapour flow rate, kg-mol s<sup>-1</sup>
  - G Defined by eqn. (9.39)
  - G' Vapour flow rate per unit bubbling area, kg-mol s<sup>-1</sup> m<sup>-2</sup>
  - $G_{ii}$  Matrix coefficients defined by eqn. (10.8)
    - q Acceleration due to gravity, m s<sup>-2</sup>
  - H Vapour enthalpy, kJ (kg-mol)<sup>-1</sup>
  - H Defined by eqn. (9.39)
  - h Liquid enthalpy, kJ (kg-mol)<sup>-1</sup>
  - h Distance from tray floor, m
  - $\Delta h(i)$  Height increment at height h(i), m
    - h<sub>cl</sub> Clear liquid height, m
  - $h_{\rm clD}$  Dynamic liquid head at tray floor, m
  - $(h_{cl})_{ow}$  Height of clear liquid flowing over weir, m
    - h<sub>cli</sub> Clear liquid height at liquid entry, m
    - $h_{co}$  Height of clear liquid in exit calming zone, m
    - $h'_{de}$  Head loss for liquid flowing under splash baffle, m of liquid
    - $h_{DT}$  Dry tray pressure drop, m of liquid
    - $h'_{DT}$   $h_{DT} + h_{R}$ , m of liquid
      - h<sub>f</sub> Height of two-phase dispersion on tray, m
    - $h_{\rm fd}$  Froth height in downcomer, m
  - $h_G$ ,  $h_1$  Heat transfer coefficients in vapour and liquid phases, kW m<sup>-2</sup> K<sup>-1</sup>
    - h, Depth of liquid at liquid entry, m
    - h<sub>i</sub> Jet height, m
    - $h_{\rm L}$  Depth of liquid in vessel, m
    - $h_{\rm m}$  Head of liquid measured by manometer, m of liquid
    - $h_n$  Pressure increase across the nappe, m of liquid
    - $h_{ow}$  Height of froth flowing over weir, m
    - $h_{\rm R}$  Residual pressure drop, m of liquid
    - $h_{\rm udc}$  Pressure drop for flow under downcomer, m of liquid
      - h<sub>w</sub> Weir height, m



#### Nomenclature xviii Wet (or total) tray pressure drop, m of liquid Clearance under downcomer, m $h_1$ $h_1, h_2$ Depth of liquid at positions 1 and 2, m i Height increment number j Drop subgroup number K Coefficient in eqn. (4.20) $K_{ni}$ Ideal solution K value for component i on tray n Overall mass transfer coefficient based on vapour, kg-mol s<sup>-1</sup> m<sup>-2</sup> $K_{\rm OG}$ $K'_{OG}$ Overall mass transfer coefficient based on vapour, m s<sup>-1</sup> $K_{\rm w}$ Parameter used in eqn. (4.10) $K_1, K_2$ Constants in eqn. (5.17) k Correction factor, eqn. (3.17) Correction factor, eqn. (3.32) k<sub>G</sub> Vapour phase mass transfer coefficient, kg-mol s<sup>-1</sup> m<sup>-2</sup> Vapour phase mass transfer coefficient, m s<sup>-1</sup> Liquid phase mass transfer coefficient, kg-mol s<sup>-1</sup> m<sup>-2</sup> $k_{\rm L}$ $k'_L$ Liquid phase mass transfer coefficient, m s<sup>-1</sup> L Liquid flow rate, kg-mol $s^{-1}$ $L_0$ Liquid flow rate on tray in absence of entrainment or weeping, Figs. 9.11, 9.14, kg-mol s<sup>-1</sup> $L_{\rm w}$ Weeping rate, kg-mol s<sup>-1</sup> Weeping rate per unit tray area, kg-mol s<sup>-1</sup> m<sup>-2</sup> l Latent heat, kJ (kg-mol) $^{-1}$ l Maximum valve lift, mm 1 Parameter in eqn. (2.32), m M Molecular weight, kg (kg-mol)<sup>-1</sup> $M_G$ Vapour flow rate, kg s<sup>-1</sup> Liquid flow rate, kg s<sup>-1</sup> $M_{\mathrm{L}}$ Valve mass, kg $M_{ m V}$ Slope of equilibrium line (binary) $\Delta v/\Delta x$ defined variously by eqns. (10.2), (10.4), (10.6) m Molar flux, kg-mol s<sup>-1</sup> m<sup>-2</sup> NNumber of completely mixed liquid pools N $N_{\mathsf{A}}$ Number of actual trays Number of binary vapour phase transfer units $N_{\rm G}$ Number of binary liquid phase transfer units, eqn. (8.12) $N_{\rm L}$ Number of binary liquid phase transfer units, eqn. (8.22) $N_{ m L}'$ Number of overall binary vapour phase transfer units $N_{\rm OG}$ $N_{\mathfrak{v}}$ Total rate of drop generation per unit tray area, m<sup>-2</sup> s<sup>-1</sup> $N_{\mathrm{T}}$ Number of theoretical trays Tray number from bottom of column



Nomenclature xix

- n Total number of bubble subgroups
- n Number of holes in area  $A_b$
- n Parameter in eqn. (2.26)
- n Parameter describing jet shape, eqn. (2.17)
- $n_1, n_2$  Number of light and heavy valves, respectively
  - P Pressure, N m<sup>-2</sup>
  - $P_{\rm b}$  Pressure within bubble, N m<sup>-2</sup>
  - P<sub>c</sub> Chamber pressure, N m<sup>-2</sup>
  - P<sub>1</sub> Excess pressure in bubble due to liquid inertia, N m<sup>-2</sup>
  - P<sub>s</sub> Pressure above liquid surface, N m<sup>-2</sup>
  - $\Delta P_R$  Residual pressure drop, N m<sup>-2</sup>
    - $P_1^d$  Pressure at position 1 for dry tray, N m<sup>-2</sup>
    - $P_1^{\text{w}}$  Pressure at position 1 for wet tray, N m<sup>-2</sup>
- $\Delta P_{12}$  Pressure difference between 1 and 2, N m<sup>-2</sup>
  - Pe Liquid Peclét number,  $Q_LD/Wh_{cl}De$  for two-dimensional model or  $Q_LZ/Wh_{cl}De$  for one-dimensional model
  - Pe<sub>G</sub> Vapour Peclét number
    - p Hole pitch, m
  - $Q_G$  Gas or vapour flow rate, m<sup>3</sup> s<sup>-1</sup>
  - $Q_F$  Froth flow rate, m<sup>3</sup> s<sup>-1</sup>
  - $Q_h$  Gas flow rate through hole, m<sup>3</sup> s<sup>-1</sup>
  - $Q_L$  Liquid flow rate, m<sup>3</sup> s<sup>-1</sup>
  - $Q_n$  Rate of heat loss from tray n to the surroundings, kW
  - *a* Heat flux, kW m<sup>-2</sup>
  - R<sub>h</sub> Hydraulic radius, m
  - Ref Reynolds number for flowing two-phase mixture
  - Reh Reynolds number for vapour flow through hole
    - r Bubble radius, m
    - r Ratio of  $N_1$  to total flux
    - r<sub>h</sub> Hole radius, m
    - $r_{\rm m}$  Manometer tube radius, m
    - $r_n$  Fraction of heat lost by vapour from tray n
    - S Stabilisation index,  $N m^{-1}$  or  $N^2 m^{-2}$
    - S Effective liquid flow path width for circular tray, m
- SF System factor
- $Sc_{\rm G}, Sc_{\rm L}$  Schmidt number  $(\mu_{\rm G}/\rho_{\rm G}D_{\rm G})$  or  $\mu_{\rm L}/\rho_{\rm L}D_{\rm L}$ 
  - s Distance of bubble centre from tray surface, m
  - s Parameter in drop size distribution, eqn. (2.33)
  - s Distance normal to curved wall, m
  - s' Parameter in drop size distribution, eqn. (2.31)
  - T Temperature, K
  - $T_{Ln}$  Temperature of liquid leaving tray n, K



## xx Nomenclature

- $T_{Ln}^*$  Bubble point temperature of liquid leaving tray n, K
  - $T_{\rm s}$  Tray spacing, m
- $T_{Vn}$  Temperature of vapour leaving tray n, K
- $T_{Vn}^*$  Dew point temperature of vapour leaving tray n, K
  - t Time, s
  - t Tray thickness, m
  - t<sub>G</sub> Mean residence time of vapour in dispersion, s
  - t<sub>L</sub> Mean residence time of liquid on tray, s
  - u Gas velocity in jet, m s<sup>-1</sup>
  - $u_{\rm b}$  Bubble rise velocity, m s<sup>-1</sup>
- $u_{\rm b0}$  Terminal rise velocity of isolated bubble, m s<sup>-1</sup>
- $u_{\rm d}$  Liquid velocity in downcomer on vapour-free basis, m s<sup>-1</sup>
- $u_{\rm dc}$  Critical value of  $u_{\rm d}$  for downcomer choking, m s<sup>-1</sup>
- $u_{\rm f}$  Mean horizontal froth velocity, m s<sup>-1</sup>
- $u_{\rm G}$  Mean vapour velocity through dispersion, m s<sup>-1</sup>
- $u_h$  Gas velocity through hole(s), m s<sup>-1</sup>
- $u_{\rm L}$  Mean liquid velocity across tray, m s<sup>-1</sup>
- $u_{L1}$  Liquid velocity at position 1, m s<sup>-1</sup>
  - $u_s$  Superficial vapour velocity based on  $A_h$ , m s<sup>-1</sup>
  - $u'_{\rm s}$  Superficial vapour velocity based on  $A_{\rm n}$ , m s<sup>-1</sup>
- $u_{\rm smax}$  Maximum value of  $u_{\rm s}$ , m s<sup>-1</sup>
- $(u_s)_{OBP}$ ,  $(u_s)_{CBP}$  Value of  $u_s$  at open and closed balance points, m s<sup>-1</sup>
  - V<sub>b</sub> Bubble volume, m<sup>3</sup>
  - V<sub>c</sub> Chamber volume, m<sup>3</sup>
  - $V_i$  Liquid molar volume at normal boiling point, cm<sup>3</sup> (g-mol)<sup>-1</sup>
  - v Drop velocity, m s<sup>-1</sup>
  - $v_0$  Fraction of open valves
  - $v_{\rm p}$  Drop projection velocity, m s<sup>-1</sup>
  - W Weir length, m
  - We Weber number
  - $w, w_1 \quad w = w'/D, w_1 = W/2D$ 
    - w' Distance from centre line measured parallel to weir, m
    - X Mole fraction in pseudo-binary liquid mixture
    - x Mole fraction in liquid
    - $x_{in}$  Tracer concentration at tracer injection point
    - $x_0$  Tracer concentration in liquid entering tray
    - $x_R$  Mole fraction in liquid leaving reboiler, Fig. 9.5
    - $x^{L}$  Mole fraction of low surface tension component  $x_{+}$  Value of x immediately downstream of liquid entry
- $x_{en-1}^*$  Mole fraction of liquid in equilibrium with vapour entering tray n
  - $\bar{x_n}$  Mean mole fraction in liquid leaving tray n via downcomer



Nomenclature xxi

- $x_n^*$  Mole fraction of liquid in equilibrium with mean vapour concentration leaving tray n
- $x'_n$  Mole fraction in liquid weeping or entrained from a point on tray n
- $\vec{x_n}$  Mean mole fraction in liquid weeping or entrained from tray *n* averaged over the tray
- Y Mole fraction in pseudo-binary vapour mixture
- $\bar{Y}_n$  Defined by eqn. (9.24) for entrainment, eqn. (9.33) for weeping
- y Depth below free surface, m
- y Parameter in eqns. (2.31), (2.33)
- y Mole fraction in vapour
- $y_n$  Value of y in vapour leaving a point on tray n
- $\bar{v}_n$  Mean value of y in vapour leaving tray n
- y\* Mole fraction in vapour which is in equilibrium with liquid
- $y_n^*$  Mole fraction in vapour in equilibrium with mean concentration of liquid leaving tray n via the downcomer
- Z Parameter in eqn. (4.19)
- Z Liquid flow path length, m
- Z<sub>e</sub> Length of exit calming zone, m
- $Z_{\rm F}$  Film thickness, m
  - z Distance normal to interface, Chapter 8, m
  - z = z'/D in two-dimensional model; z = z'/Z in one-dimensional model
- z' Distance from inlet weir, m
- $z_1$  Value of z at exit weir
- $z_{\rm in}$  Value of z at tracer injection point
- α Volume of liquid per unit volume of two-phase dispersion (liquid holdup fraction)
- α Relative volatility, eqn. (7.23)
- α Similarity ratio, Chapter 9
- $\alpha_d$ ,  $\bar{\alpha}_d$  Local and mean liquid volume fraction in the downcomer
  - $\alpha_e$  Effective liquid volume fraction defined by eqn. (3.24)
  - $\alpha(i)$  Local liquid volume fraction at height h(i)
  - $\alpha_R$  Liquid volume fraction in froth flowing under downcomer
- $\alpha_{OG}, \alpha_{G}, \alpha_{L}$  Parameters in eqns. (10.7)
  - $\beta_0$  Fractional weeping rate,  $L_w/L_0$ 
    - γ Parameter in eqns. (10.10)
  - $y_{ni}^{L}$  Activity coefficient of component i in liquid leaving tray n
    - $\varepsilon$  Volume of gas or vapour per unit volume of two-phase dispersion (gas holdup fraction)
  - $\varepsilon_{\rm w}$  Value of  $\varepsilon$  in froth flowing over weir
  - $\varepsilon'_1$  Local volume fraction of small bubbles
  - $\eta = \varepsilon/(1-\varepsilon)$ , eqn. (3.10)
  - $\theta$  Contact angle
  - $\theta(ij)$  Residence time of drops j in height increment at height h(i), s



### xxii Nomenclature

- $\lambda$  Stripping factor or ratio of slope of equilibrium line to slope of operating line, mG/L
- $\lambda_0 = mG/L_0$
- $\mu_G, \mu_L$  . Vapour and liquid viscosity,  $N\,s\,m^{-2}$ 
  - v Volume fraction of drops having diameter less than y, eqn. (2.31)
  - ξ Orifice coefficient
  - $\xi'$  Modified orifice coefficient, eqn. (4.18)
  - $\xi_0$  Orifice coefficient as  $\phi \to 0$ , Fig. 4.2
  - $\xi_{VC}$  Orifice coefficient for valves resting on tray deck
  - $\xi_{VD}$  Orifice coefficient for valve tray deck
  - $\xi_{Vi}$  Orifice coefficient for combination of light and heavy valves
  - $\xi_{VO}$  Orifice coefficient for open valves
  - $\rho_{\rm F}$  Density of two-phase dispersion, kg m<sup>-3</sup>
- $\rho_{\rm G}, \rho_{\rm L}$  Vapour and liquid density, kg m<sup>-3</sup>
- $\rho'_{\rm G}, \rho'_{\rm L}$  Vapour and liquid density, kg-mol m<sup>-3</sup>
  - $\rho_{\rm H,O}$  Density of water, kg m<sup>-3</sup>
    - $\sigma$  Surface tension, N m<sup>-1</sup>
- $\sigma^+, \sigma^-, \sigma^0$  Surface tension positive, negative or neutral system
  - $\phi$  Fractional perforated tray area (hole area/bubbling area); also called fractional free area
  - $\phi_A$  Association factor
    - $\psi$  Defined by eqn. (3.22a), m
  - $\psi$  Parameter in eqn. (10.5)
- $\mathcal{N}_{\text{OG}}, \mathcal{N}_{\text{G}}, \mathcal{N}'_{\text{L}}$  Number of overall vapour phase, vapour phase and liquid phase ternary transfer units

#### **Subscripts**

- b In bulk phase
- G In gas or vapour phase
  - i For bubble subgroup i
  - i For component i
  - i At interface
- ij For the binary ij
- j For the jet
- j For component j
- L In liquid phase
- n Leaving tray n
- V In vapour phase
- 1 or 2 For component 1 or 2, respectively *or* for small or large bubbles, respectively

## **Superscripts**

- e Exit stream from ideal tray
- 0 Local value at the exit weir



Nomenclature xxiii

- Mean value
- ·, · First and second derivatives with respect to time
- " Entering value used in ideal tray definition, Fig. 7.1