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Indexing of individuals is for cited theorems only. Additional information regarding individuals may be obtained from the Guide above.

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